

# Inpatient Flow Management in a Singaporean Hospital

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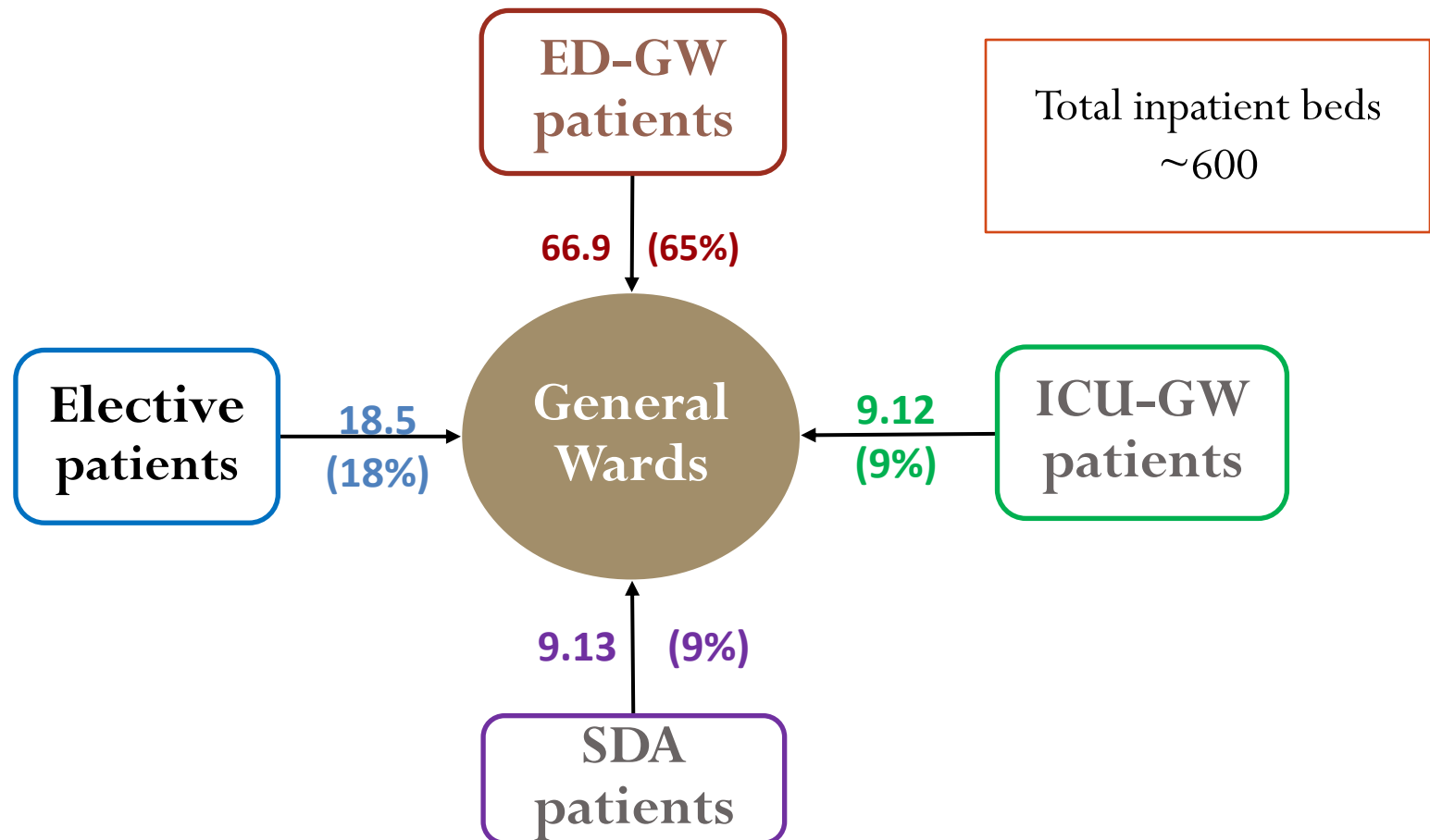
National University Hospital, Singapore

# Overview

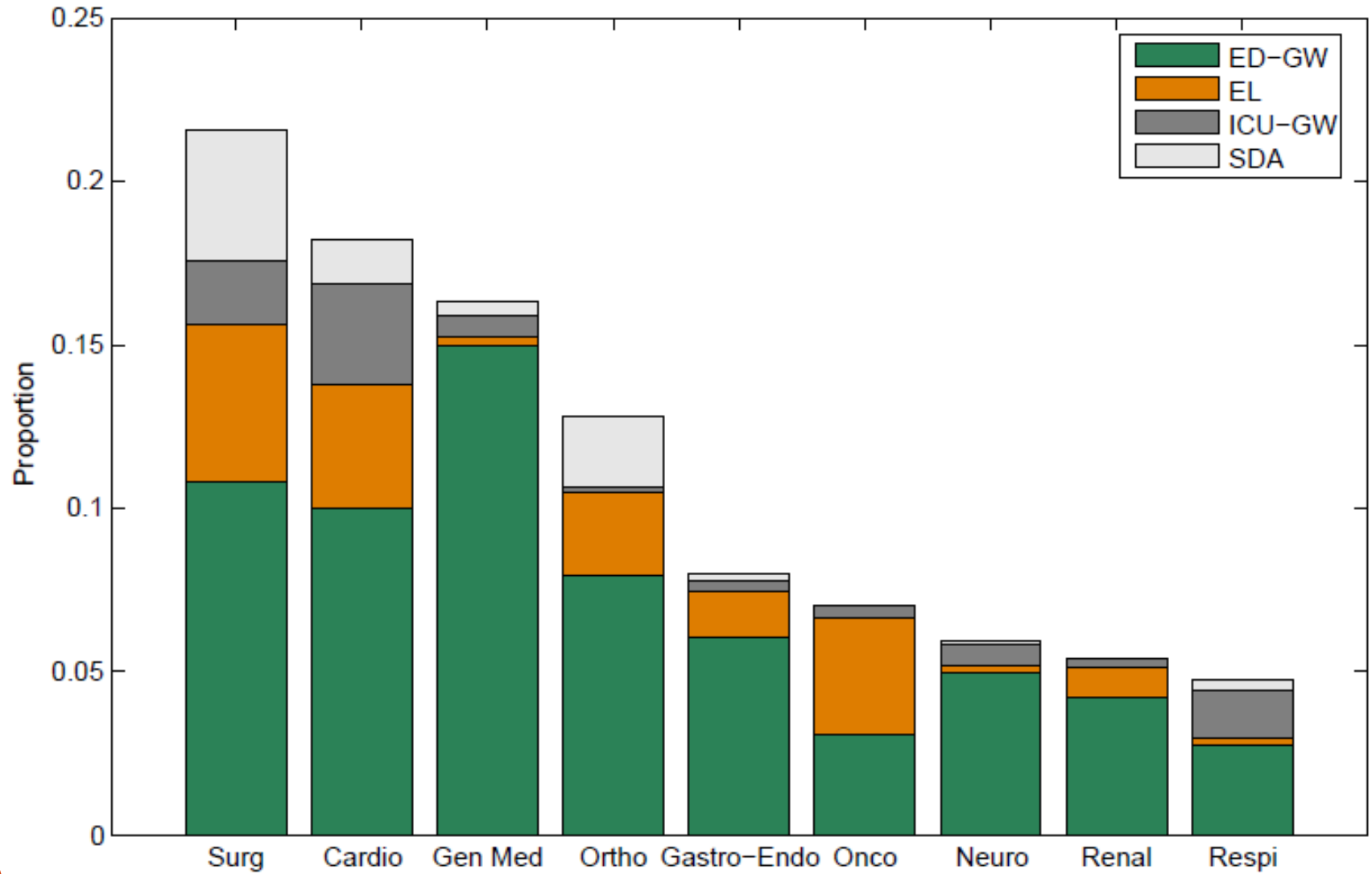
- Empirical study
  - Inpatient flow management
  - Performance comparison after an *early discharge* policy
    - Waiting time for admission to ward
    - Stabilize hourly waiting time performance
- A stochastic network model
  - Allocation delays
  - Overflow policy
  - Endogenous service times
- What-if analysis
  - Factors help to stabilize waiting time

# Capacity and source of admission

- Patients from 4 admission sources competing for inpatient beds



# Patient distribution



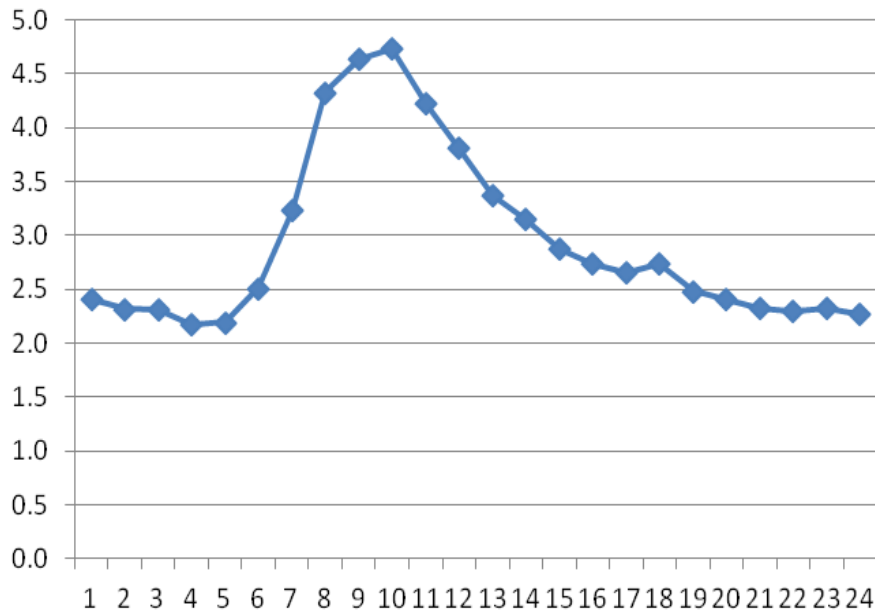
# Key performance measures

- Waiting time for admission to ward (Jan 08 – Jun 09)
  - Waiting time = admission time – bed request time
  - Average: **2.82** hour
  - **6.52%** of ED-GW patients wait more than 6 hours to get a bed
- “x-hour service level”: Fraction of ED-GW patients waiting more than x hours
  - Ministry of Health (MOH) monitors 10-hour service level (**0.80%**)
  - Hospital managers also care about the 6-hour service level

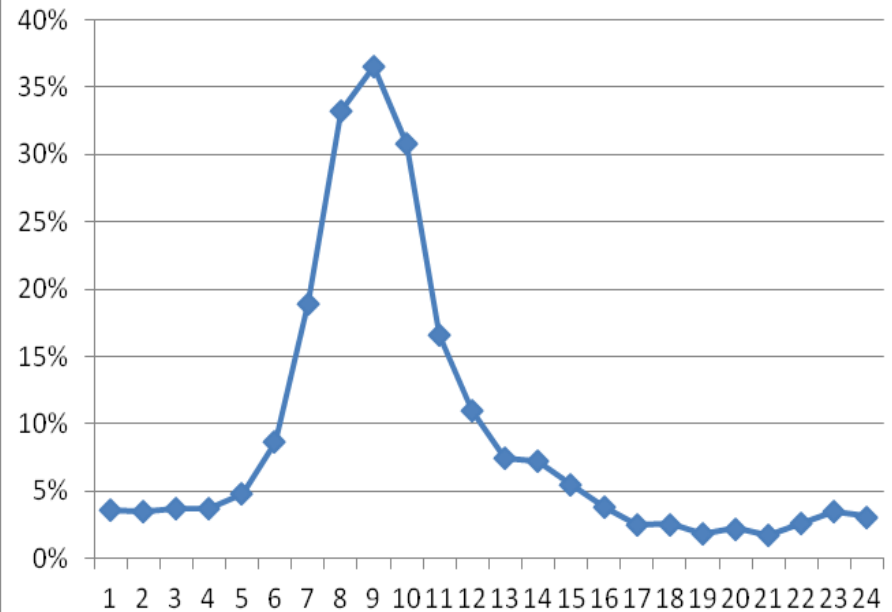
# Time dependency

- Waiting time depends on patient's bed request time
  - Jan 08 – Jun 09
  - Can we *stabilize*?

## Avg. waiting time



## 6-h service level

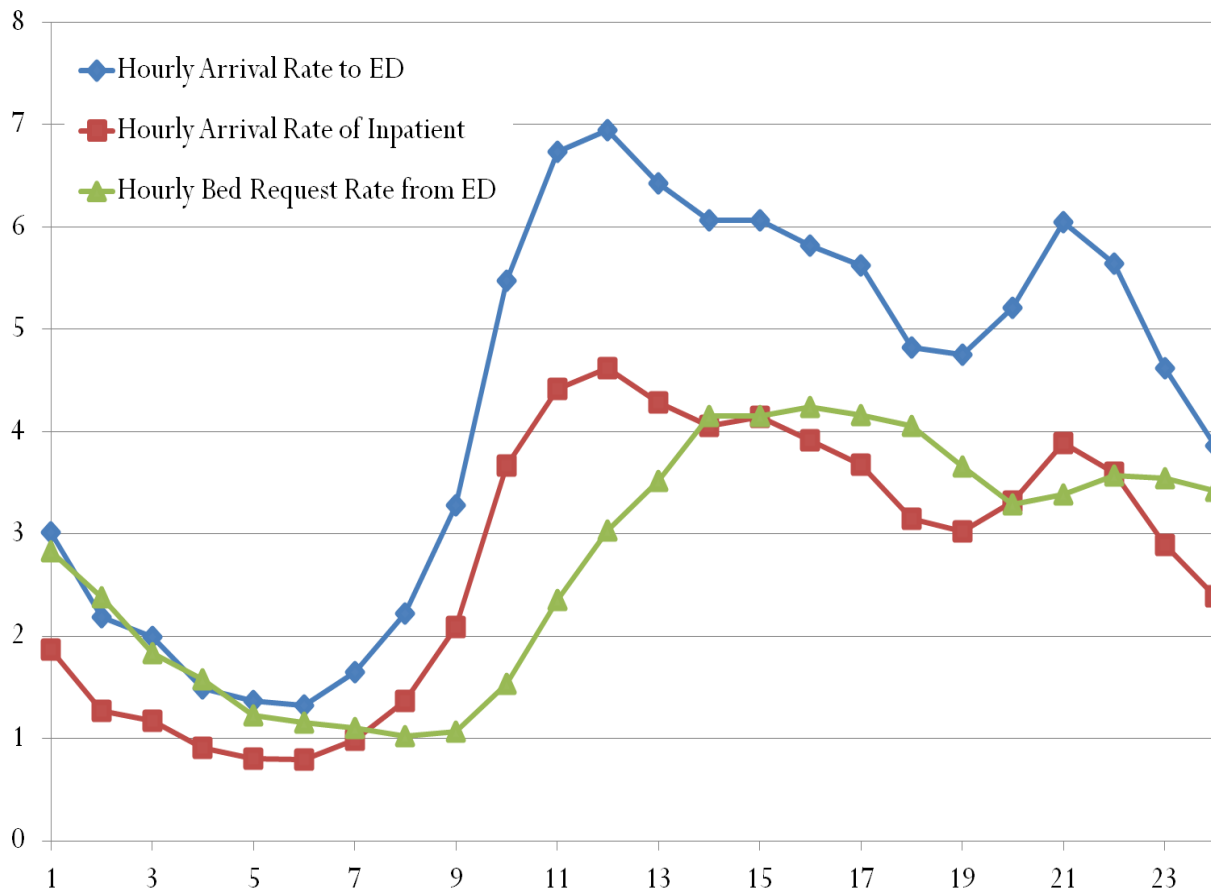


# Literature review

- Zohar Feldman, Avishai Mandelbaum, William A. Massey and Ward Whitt, *Management Sciences*, 2008.
  - **Staffing of Time-Varying Queues to Achieve Time-Stable Performance**
- E. S. Powell, R. K. Khare, A. K. Venkatesh, B. D. Van Roo, J. G. Adams, and G. Reinhardt, *The Journal of Emergency Medicine*, 2012
  - **The relationship between inpatient discharge timing and emergency department boarding**
- Affiliations: Department of Emergency Medicine, Northwestern University; Harvard Affiliated Emergency Medicine Residency, Brigham and Women's Hospital–Massachusetts General Hospital, ...

# Bed request rate and arrivals to ED

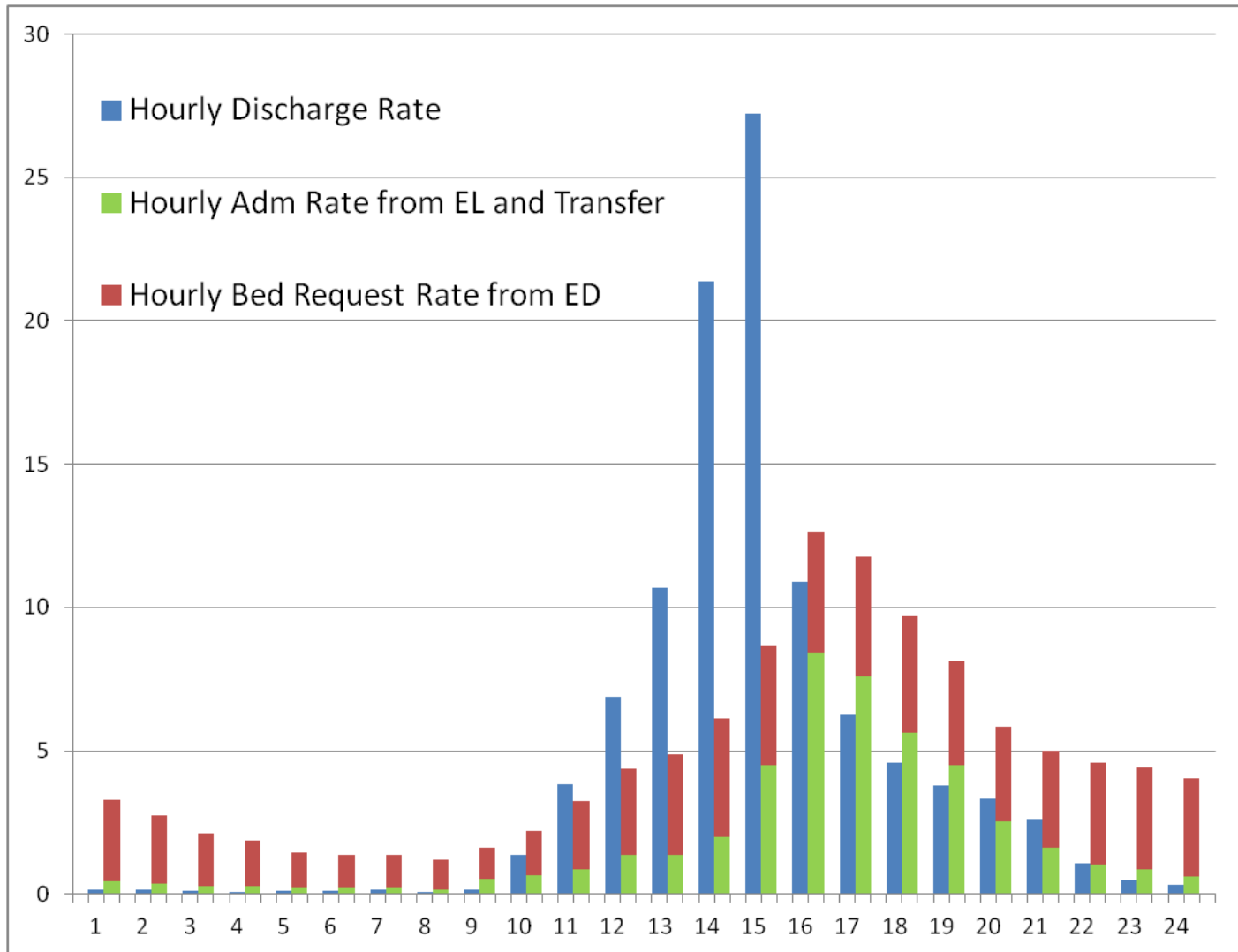
- ED-GW patient's bed request rate (**green** curve) depends on arrival rate to ED (**blue** curve)





# Mismatch between demand and supply of beds

• Jan 08 – Jun 09



# Early discharge policy

- Moving the discharge time a few hours earlier in the day
  - Safe: limited effect in increasing patient's risk
  - Costly to implement
- Recommended by many studies, policy guidelines:
  - National Health Service (NHS, UK): *“planning for a reasonable proportion of patients to leave the ward before 11 am helps to manage the total loading on beds”*
  - Intuition: moving the discharge time earlier (by even 1 or 2 hours) can improve operations and patient flow.

[1] NHS. [http://www.institute.nhs.uk/quality\\_and\\_service\\_improvement\\_tools/quality\\_and\\_service\\_improvement\\_tools/discharge\\_planning.html](http://www.institute.nhs.uk/quality_and_service_improvement_tools/quality_and_service_improvement_tools/discharge_planning.html)

[2] Achieving timely simple discharge from hospital. NHS. 2004.

[3] Discharge Planning Handbook for Healthcare: Top 10 Secrets to Unlocking a New Revenue Pipeline. 2008. Productivity Press.

[4] Discharge by Appointment: Freeing Up In-Patient Bed Capacity.

# Data

- The hospital implemented early discharge policy since July 2009

- Study two periods of data

- Jan 2008 to Jun 2009 (Period 1)

- 13% before noon

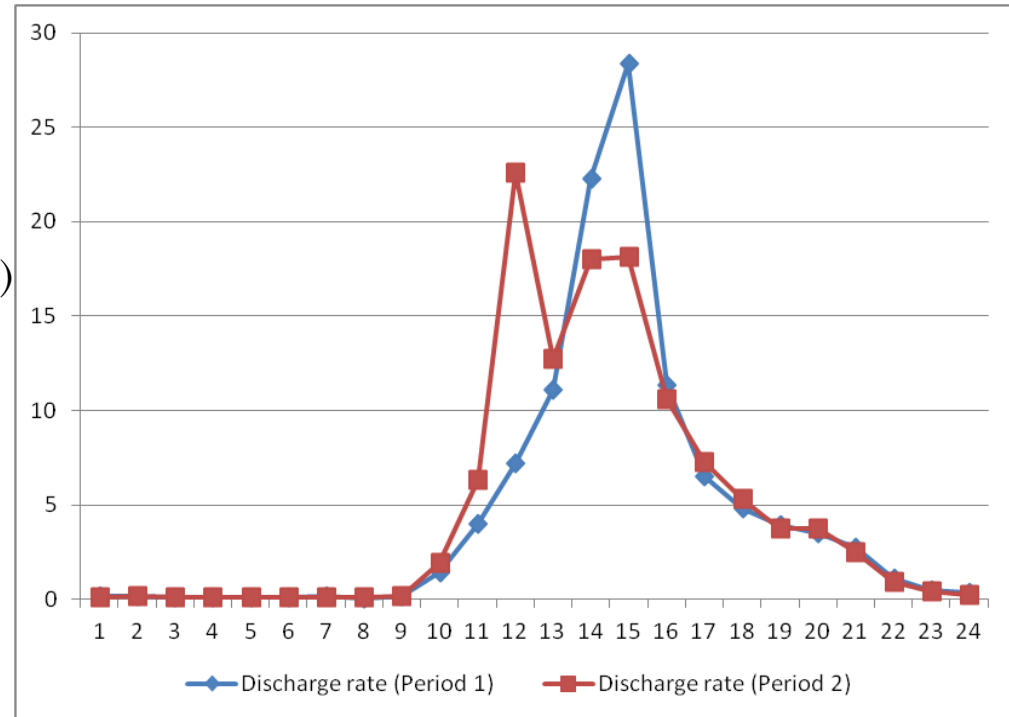
- Jan 2010 to Dec 2010 (Period 2)

- 26% before noon

- Is early discharge policy helpful?

- Empirical analyses

- Use model to evaluate



- Key performance measures in the two periods

- Waiting time statistics (quality)

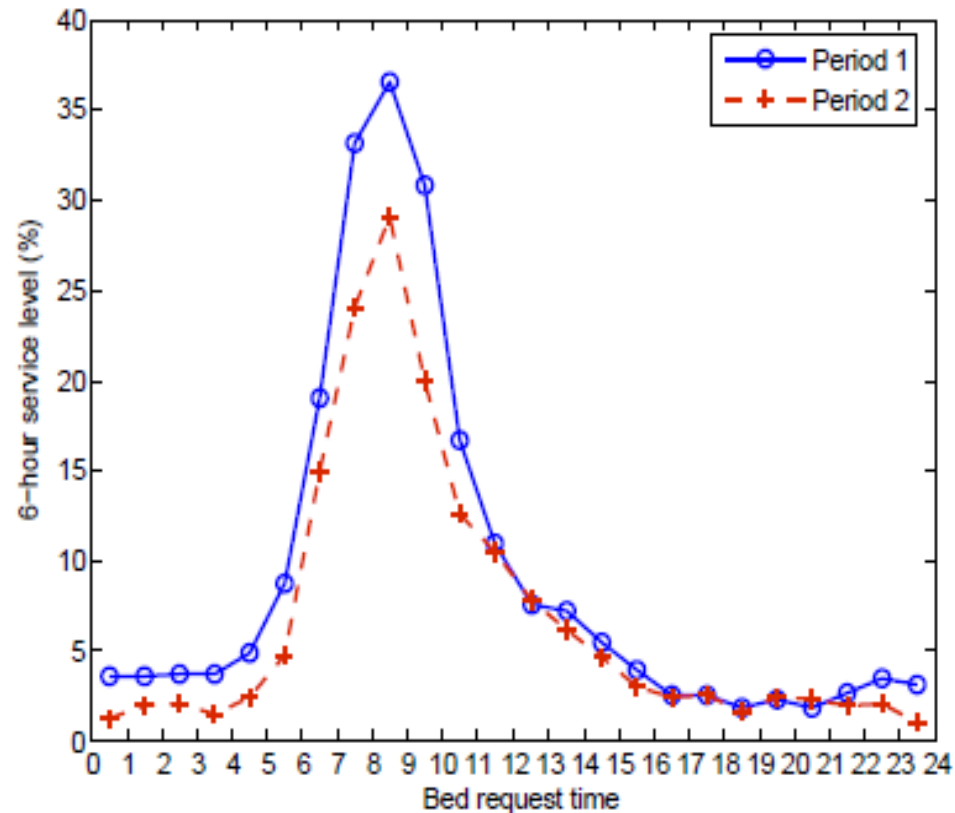
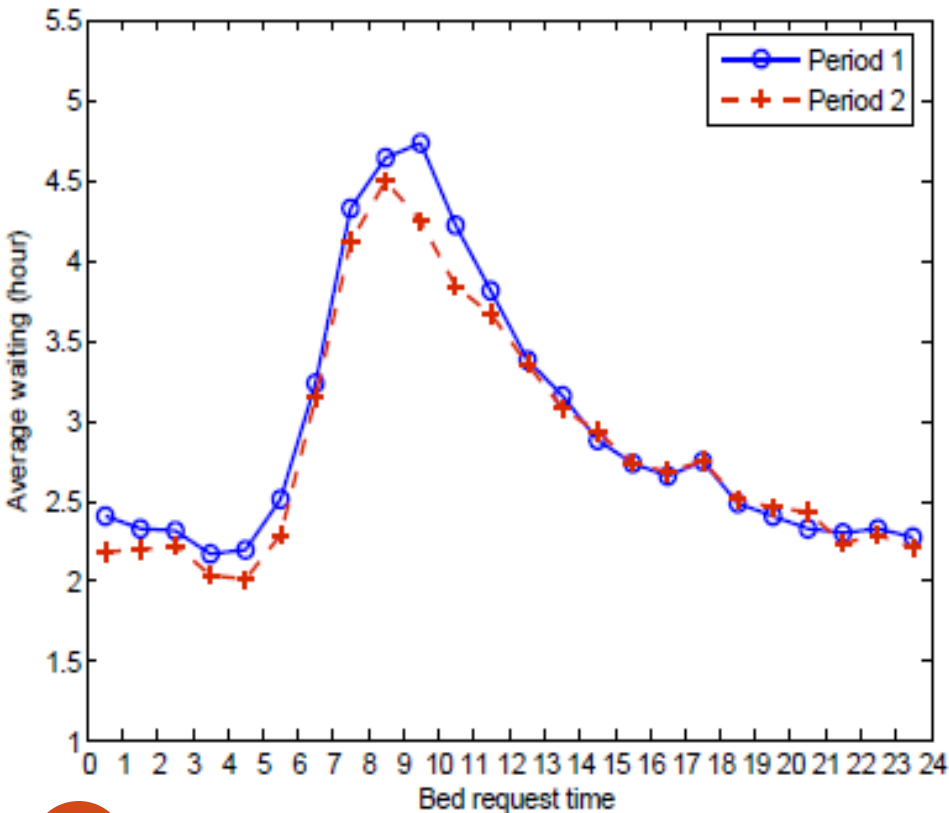
- Overflow rate (cost)

# Empirical Analysis on the two periods

- Waiting time performance
- Overflow rate
  - Period 1: 26.9%
  - Period 2: 25.0%
- BOR

# Waiting time for ED-GW patients

	1 <sup>st</sup> period	2 <sup>nd</sup> period
Average waiting time	2.82 h	2.77 h
6-hour service level	6.52%	5.13%

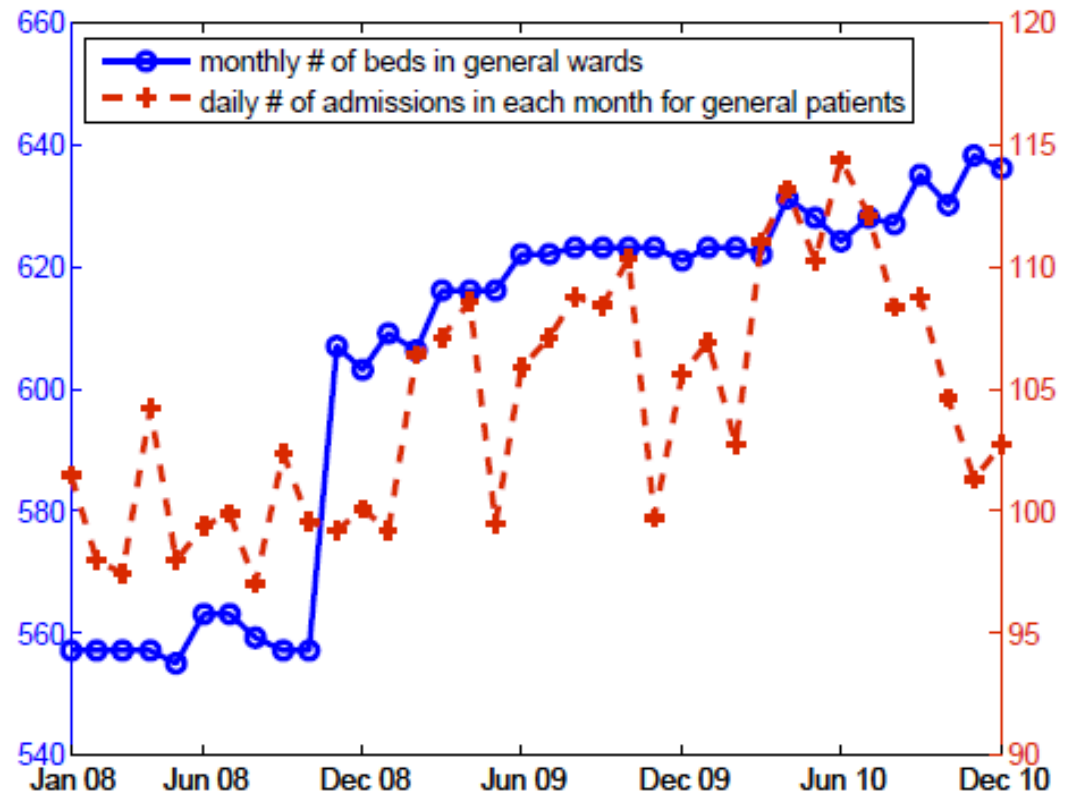


# Challenges

- Does the modest improvement come from the early discharge?
- More importantly, is any operational policy that can stabilize the waiting time?

# Unstable Environment

- Both arrival volume and capacity increases during 2008 to 2010
- Bed occupancy rate (BOR) reduces in the Period 2
  - Period 1: **90.3%**
  - Period 2: **87.6%**



- Need a model to help evaluate the effect of early discharge

# A stochastic model

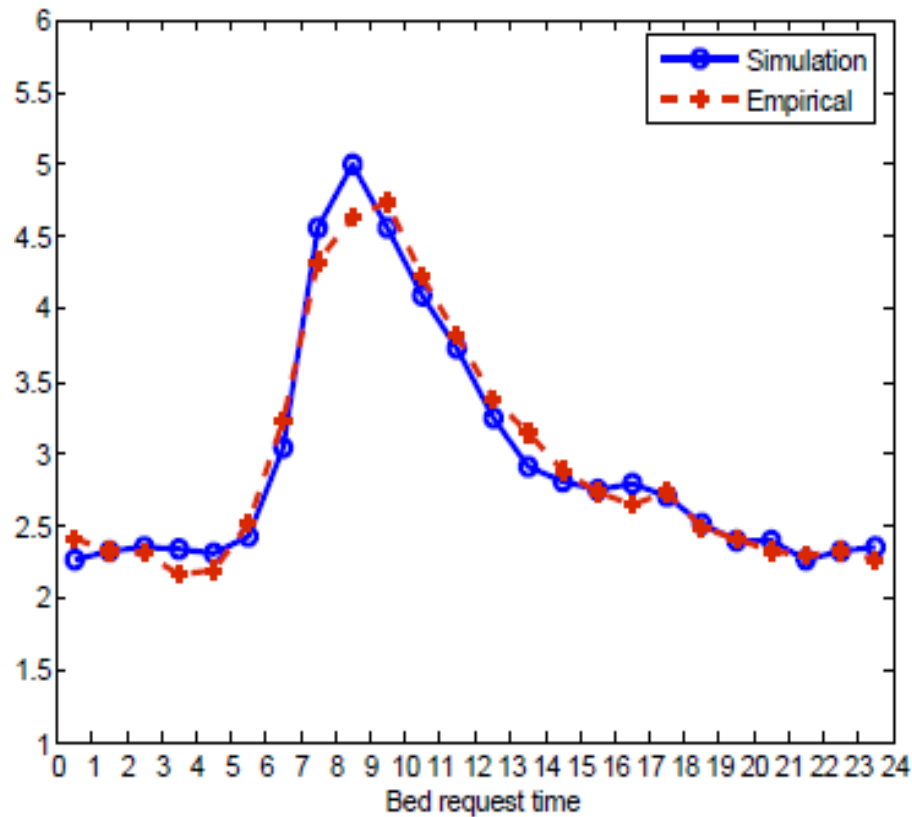
- Multi-class, multi-server pool system
  - Each server pool is either dedicated to one class of customer or flexible to serve two and more classes of customers
- Periodic arrival
  - 4 types of arrival (ED-GW, Elective, ICU-GW, SDA) for each specialty
- A novel service time model
- And other key components



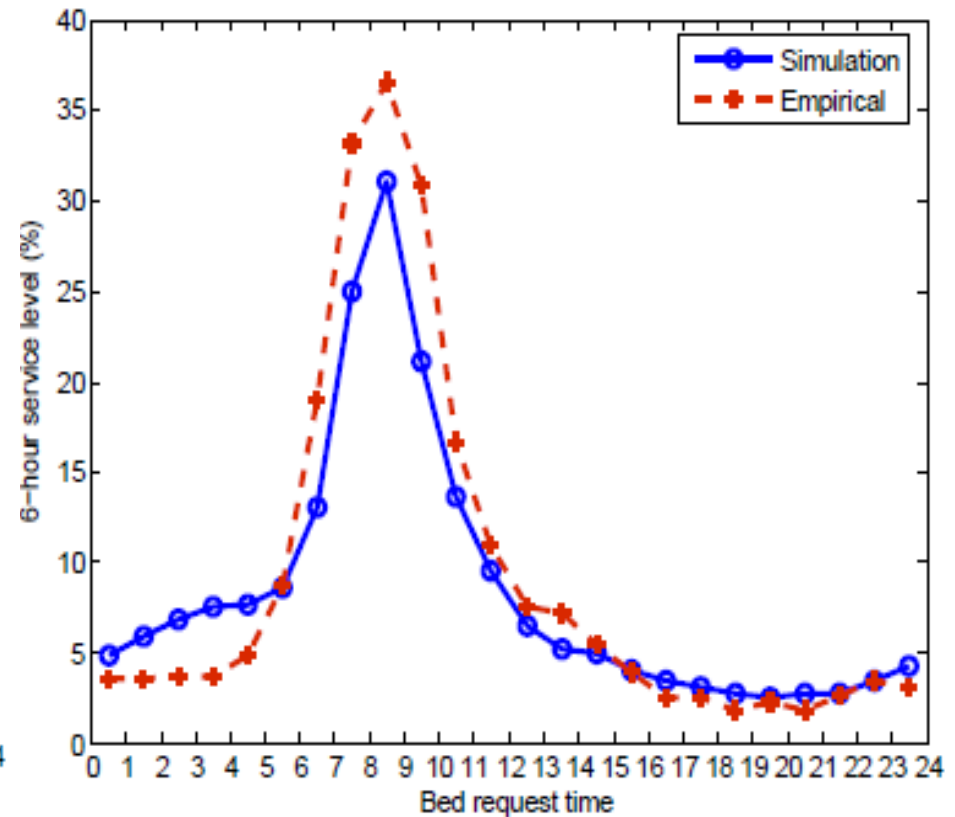
# Simulation replicates most performance measures

- Hourly waiting time performances

(a) Hourly average waiting time



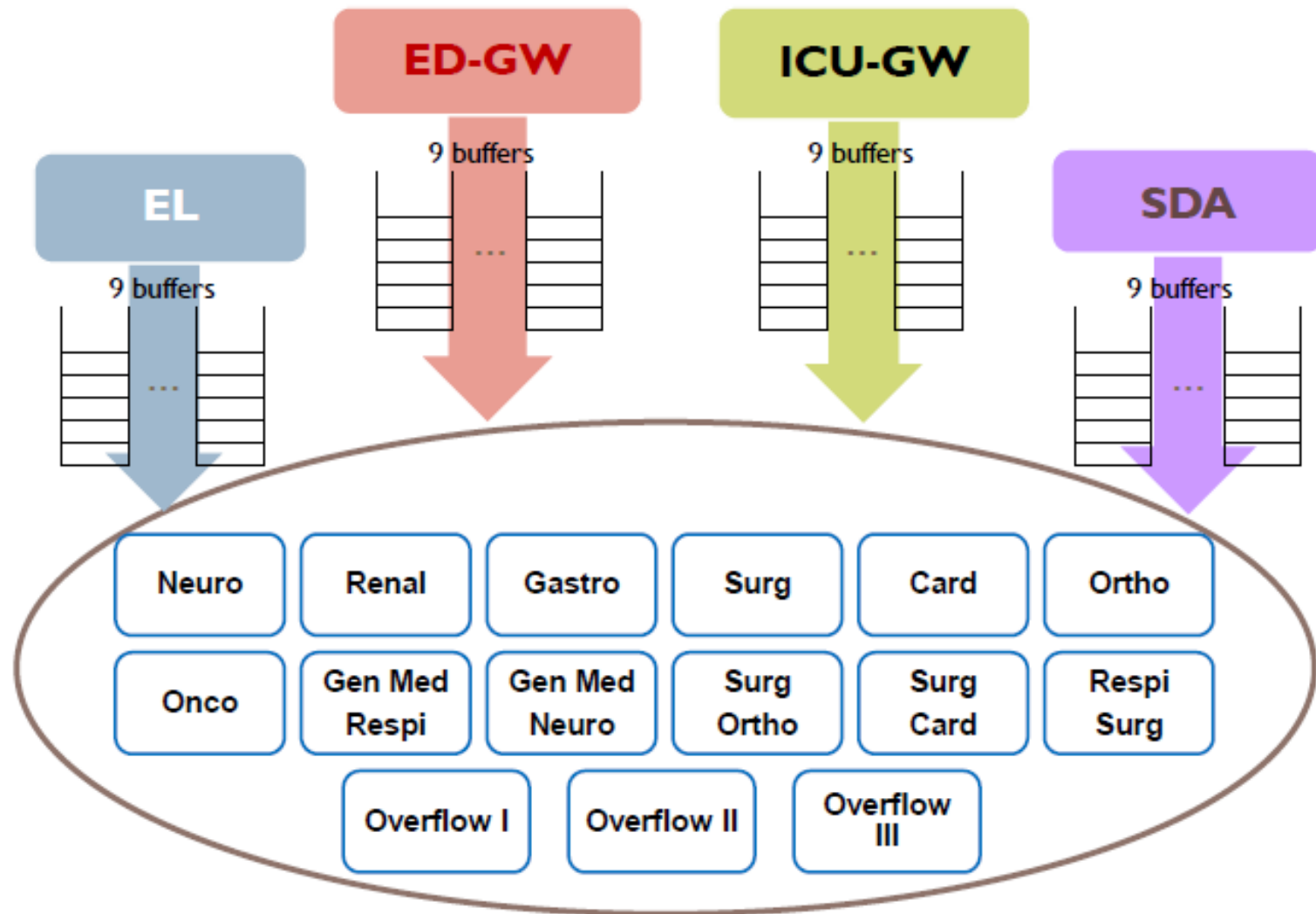
(b) Hourly 6-hour service level



# Key modeling components

- Service time model
  - Determined by admission time, **LOS** and discharge distribution
  - An endogenous modeling element
  - No longer i.i.d.
- Allocation delays
  - “Secondary” bottlenecks other than bed availability
    - Yankovic and Green (2011)
    - Armony et al (2011)
- Overflow policy
  - When to overflow a patient
  - Overflow to which server pool

# Network structure



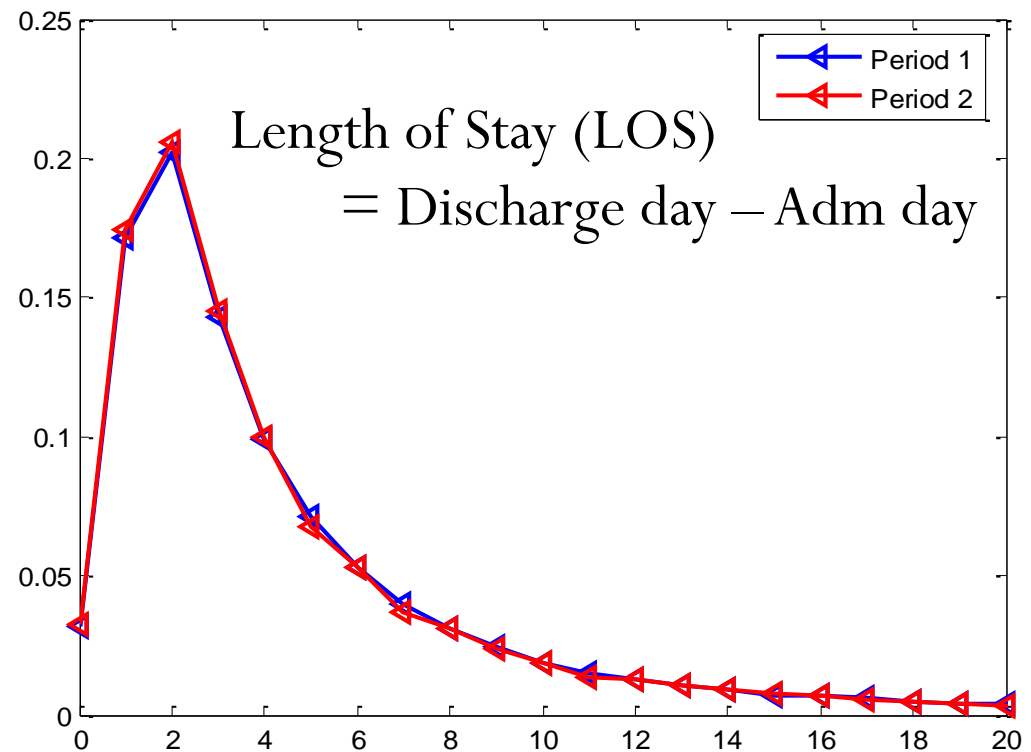
# Service time model

- Service time model

- Service time = Discharge time – Admission time  
= **LOS + Dis hour – Adm hour**

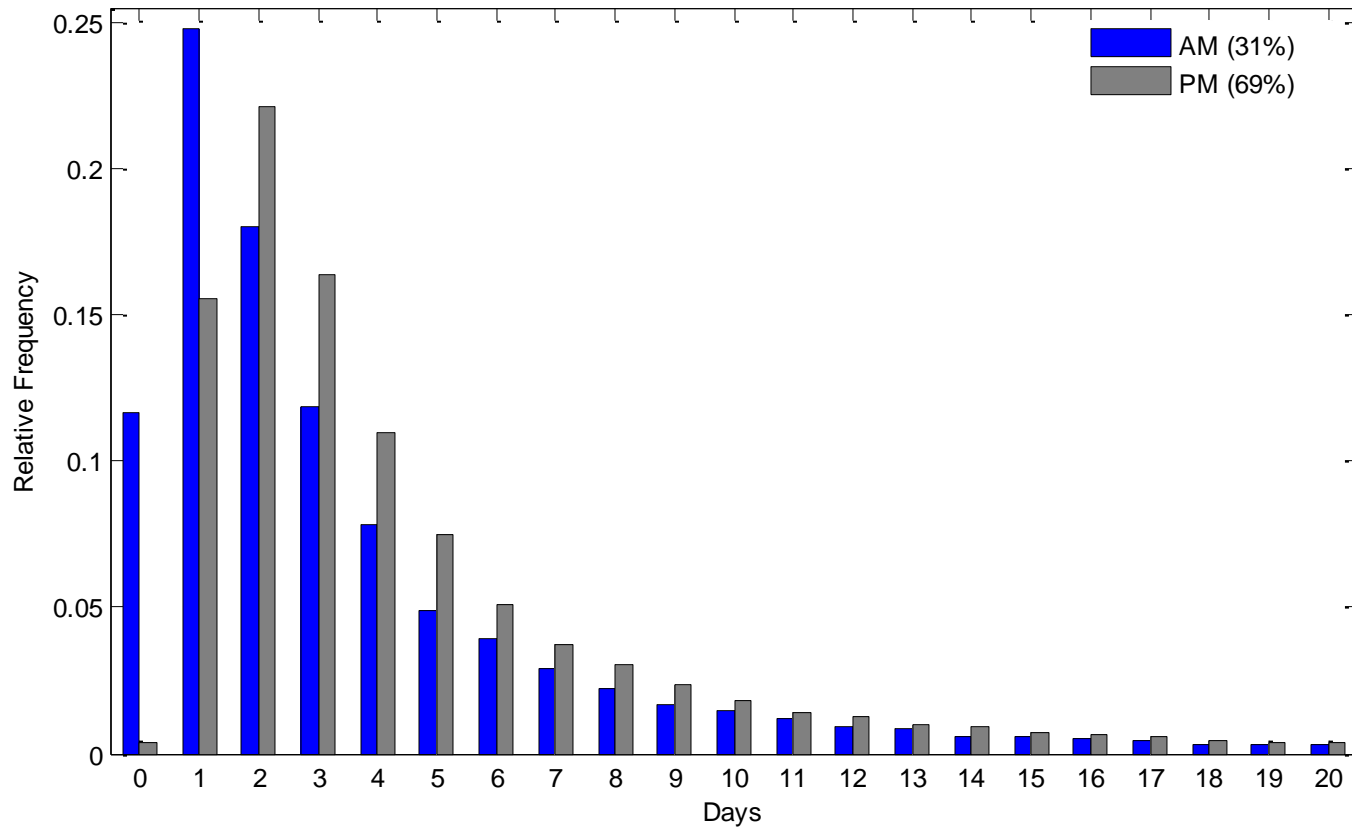
- LOS distribution

- Average is ~ 5 days
  - Depend on *admission source* and *specialty*



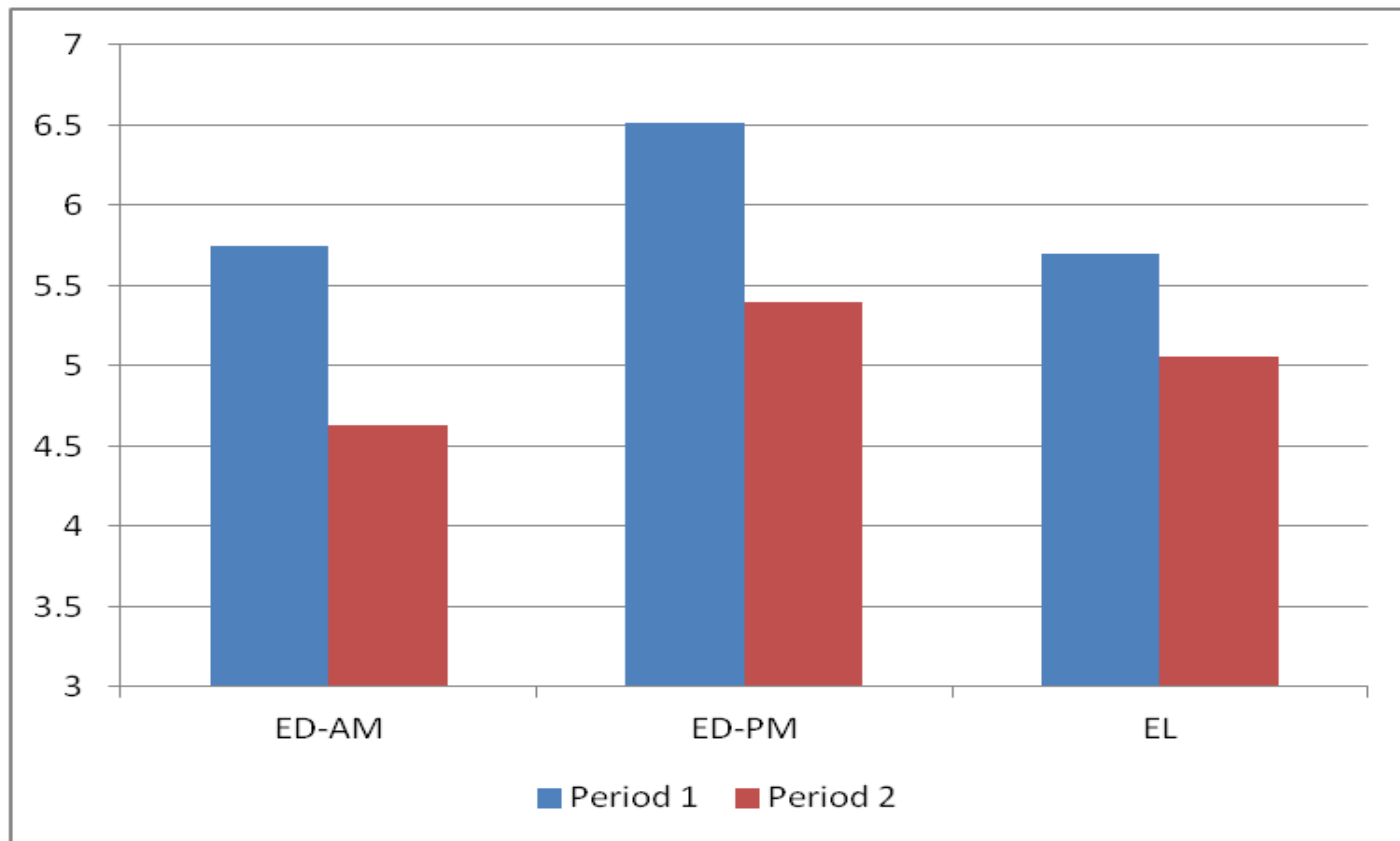
# AM PM patients (ED-GW patients)

- The admission time affects LOS
  - AM patients: average LOS = 4.24 days
  - PM patients: average LOS = 5.31 days



# Renal patients show a great reduction in Average LOS

- Average LOS is reduced by almost 1 day



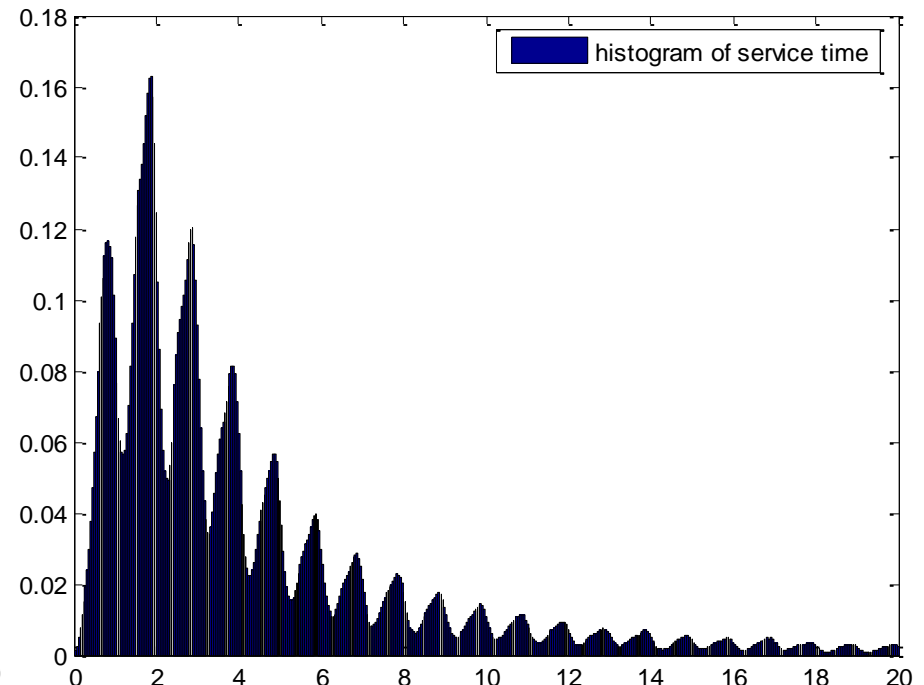
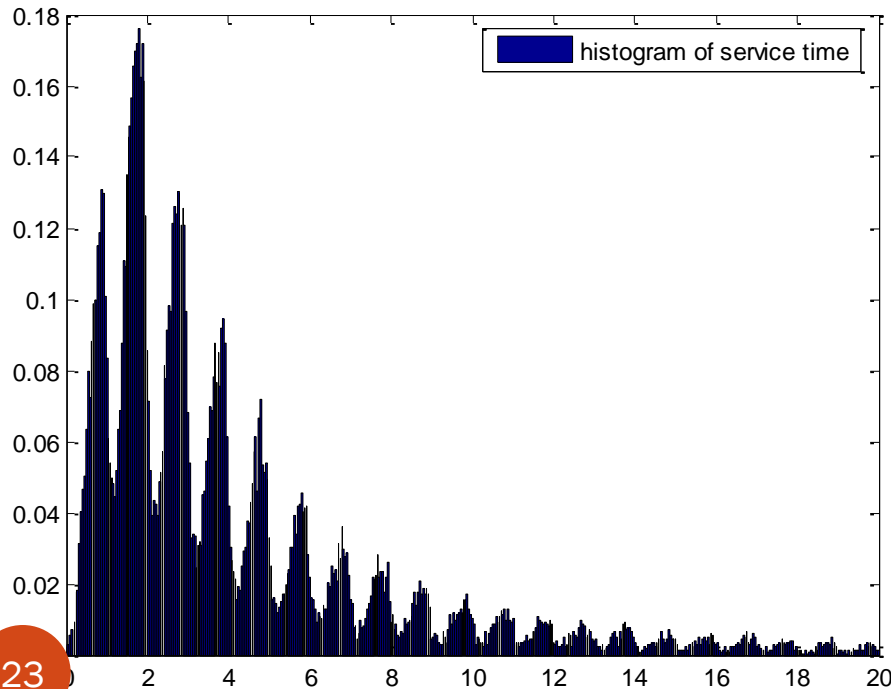
# Verify the service time model

- Service time model
  - Service time = LOS + Discharge hour – Adm hour

Matching empirical

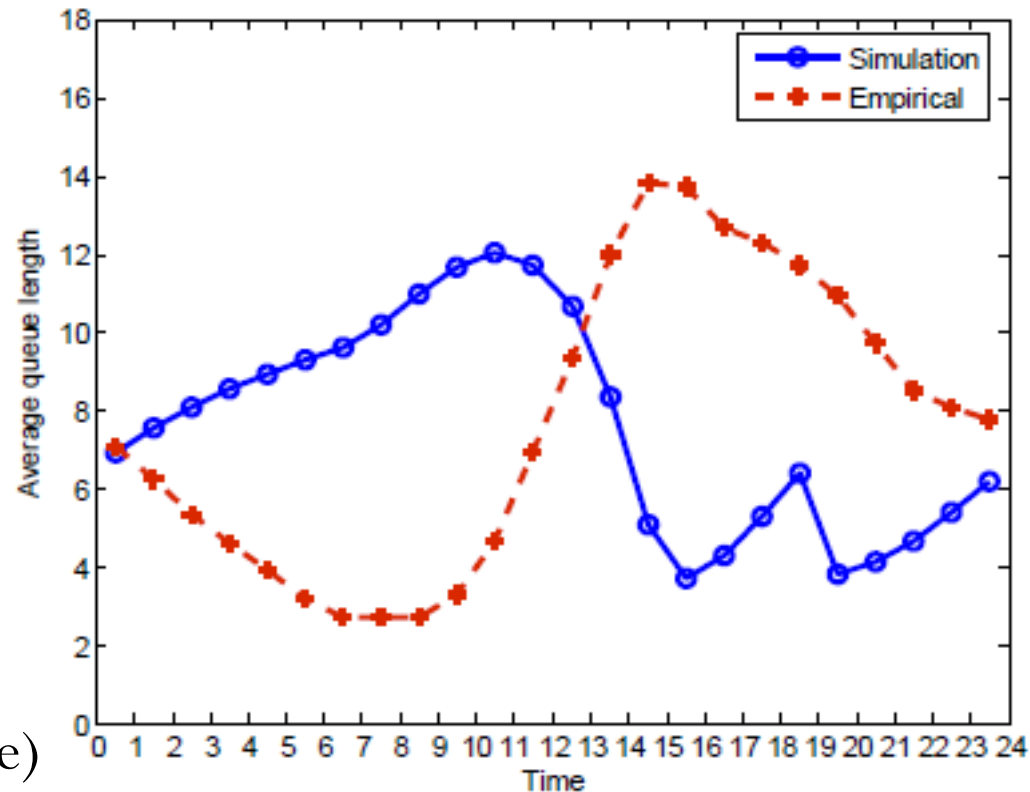
(a) Empirical

(b) Simulation output



# Pre- and post-allocation delays

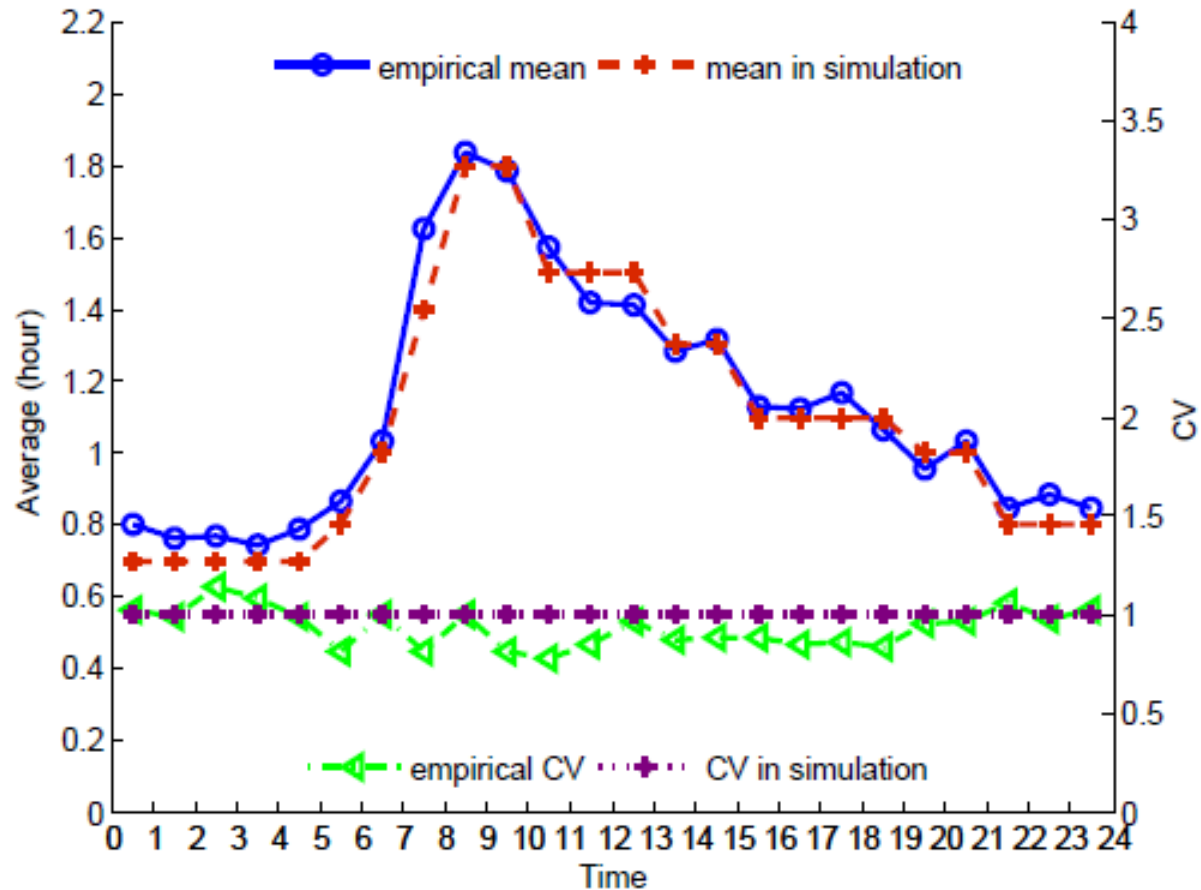
- Patient experiences additional delays upon arrival and when a bed is allocated
  - Pre-allocation delay
    - BMU search/negotiate for beds
  - Post-allocation delay
    - Delays in ED discharge
    - Delays in the transportation
    - Delays in ward admission
- Must model bed turnover component
  - If not, hourly queue length does not match (right figure)





# Time-dependent allocation delays

- The mean of allocation delay depends on when it is initiated
  - Use log-normal distribution
  - Pre-allocation delay



# Overflow policy

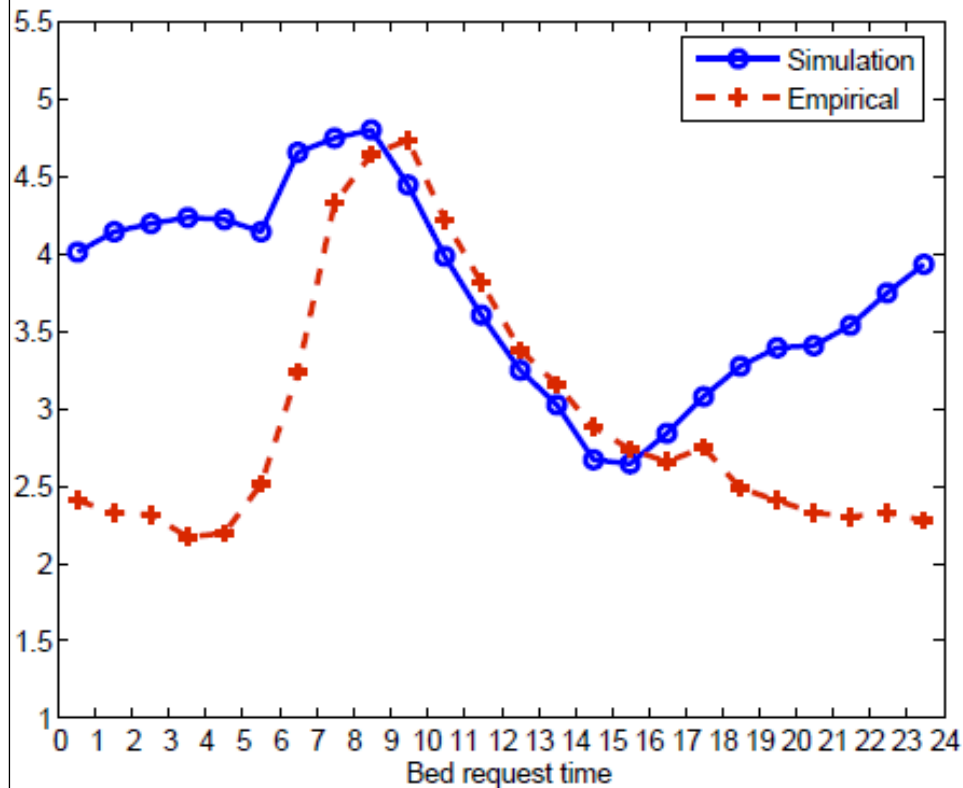
- When a patient's waiting time exceeds certain threshold, the patient can be overflowed to a “wrong” ward
  - Beds are partially flexible
  - Overflow wards have certain priority

Cluster	1 <sup>st</sup> Overflow	2 <sup>nd</sup> Overflow	3 <sup>rd</sup> Overflow
Medicine	Other Med	Surgery/OG	Ortho
Surgery	Other Surg	Ortho / OG	Medicine
Ortho	Other Ortho	Surgery	Medicine

# Dynamic overflow policy

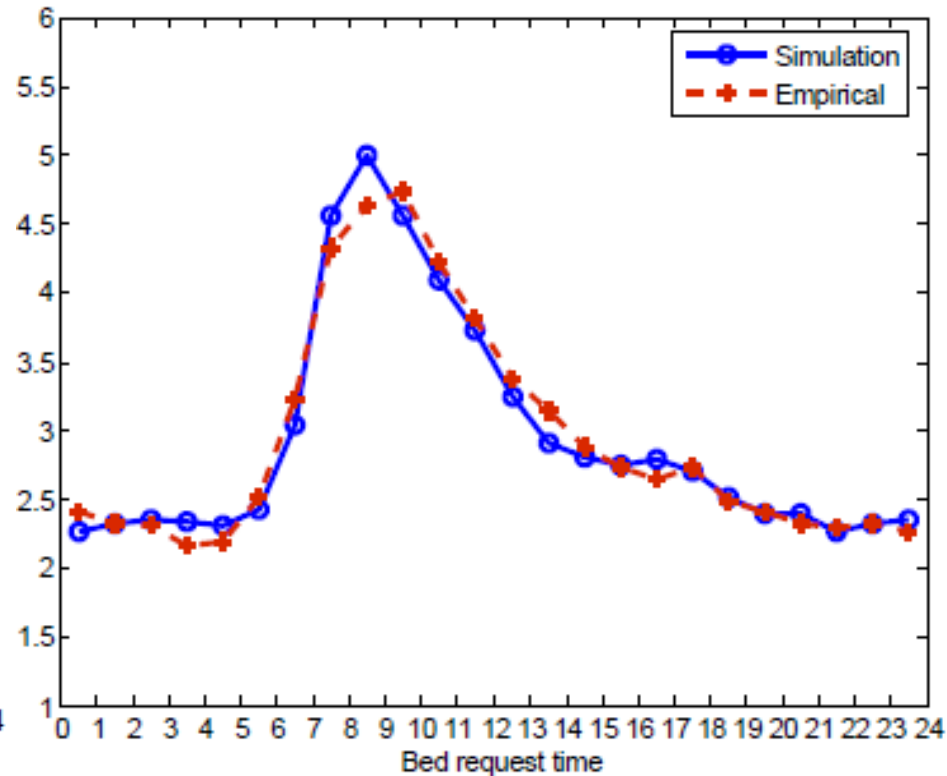
## Fixed threshold

- Threshold: 4.0 h

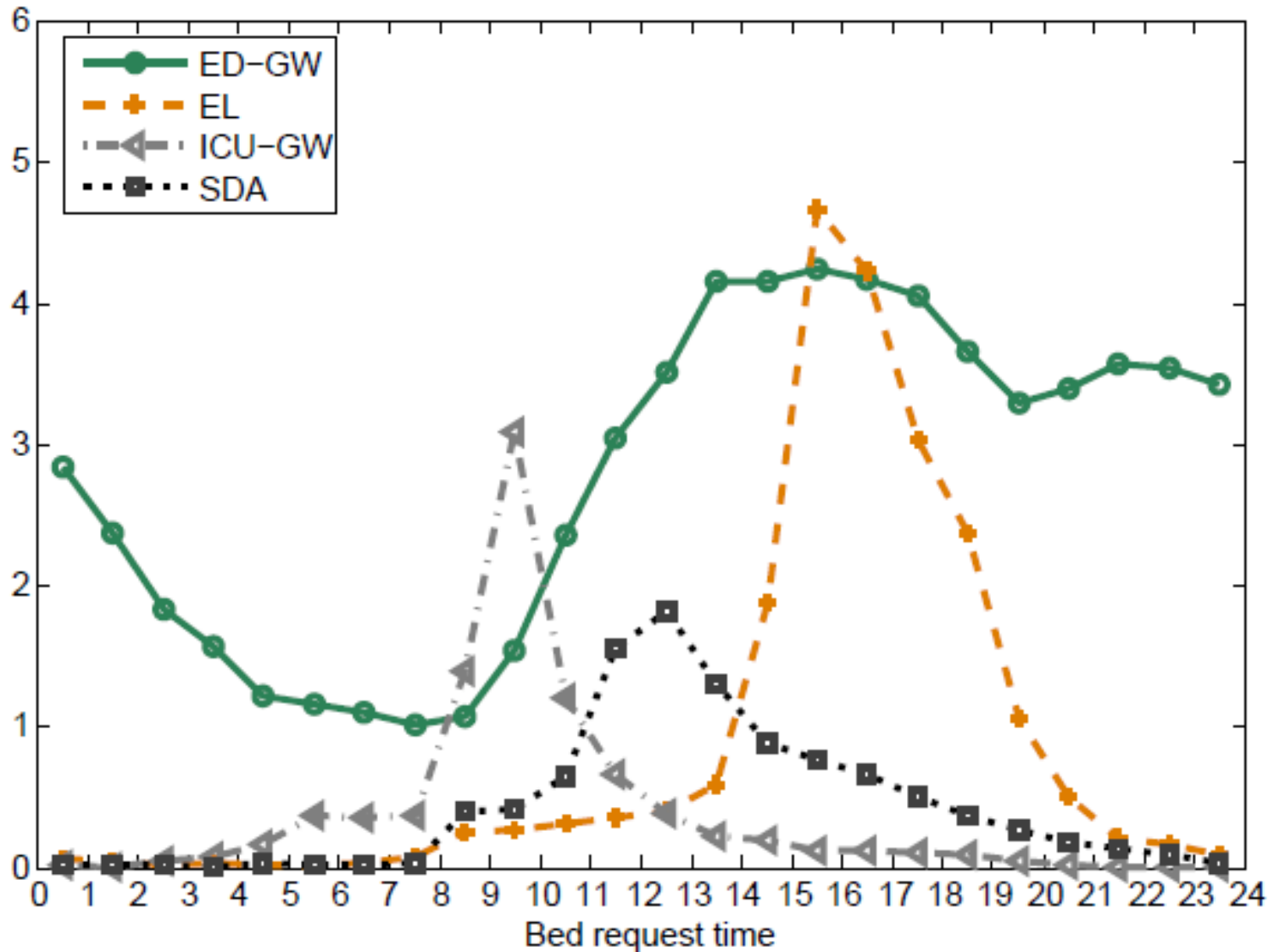


## Dynamic threshold

- Threshold: 0.5 h for arrival between 7 pm and 7 am (next day); 5.0 h for others



# Time-varying arrival rates



# Simulation results

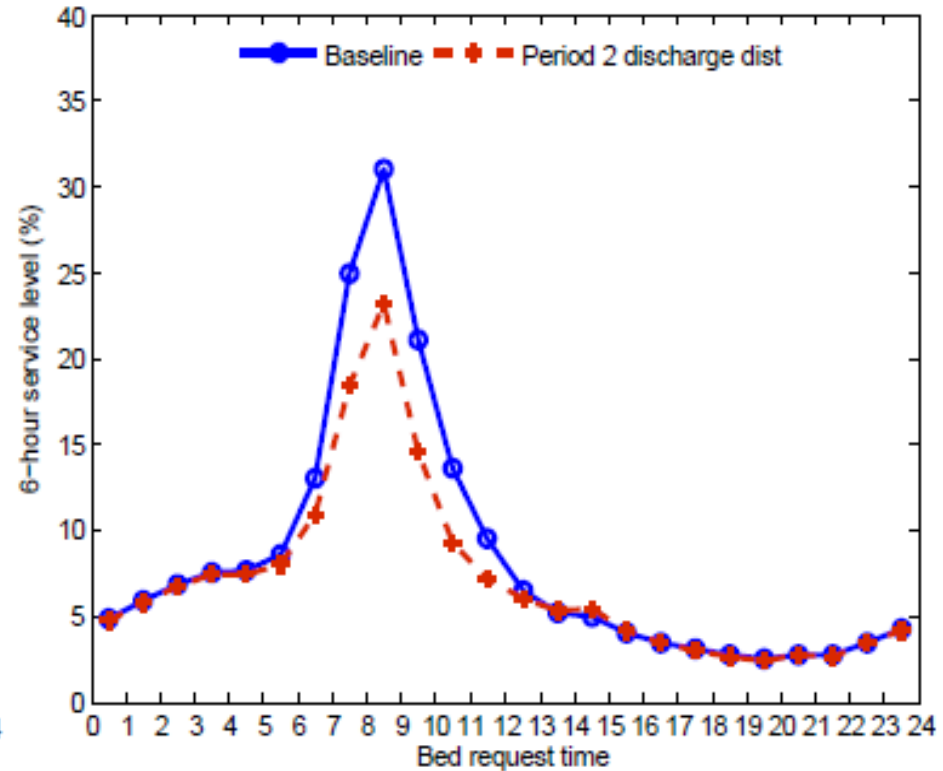
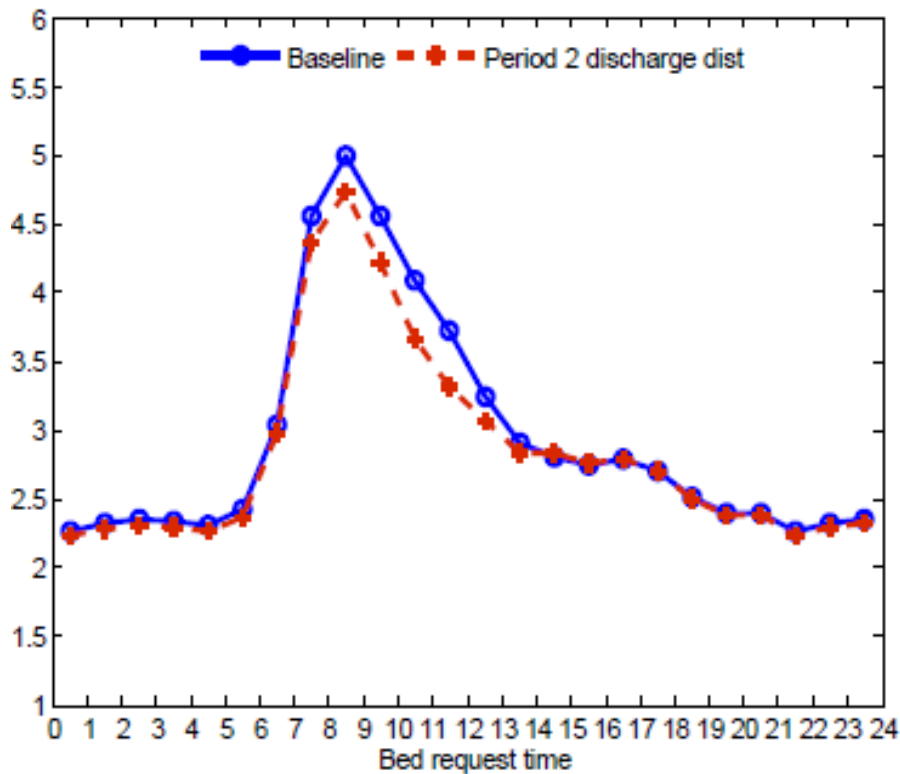
- Whether early discharge policy is beneficial or not
- What-if analysis

# Simulation results

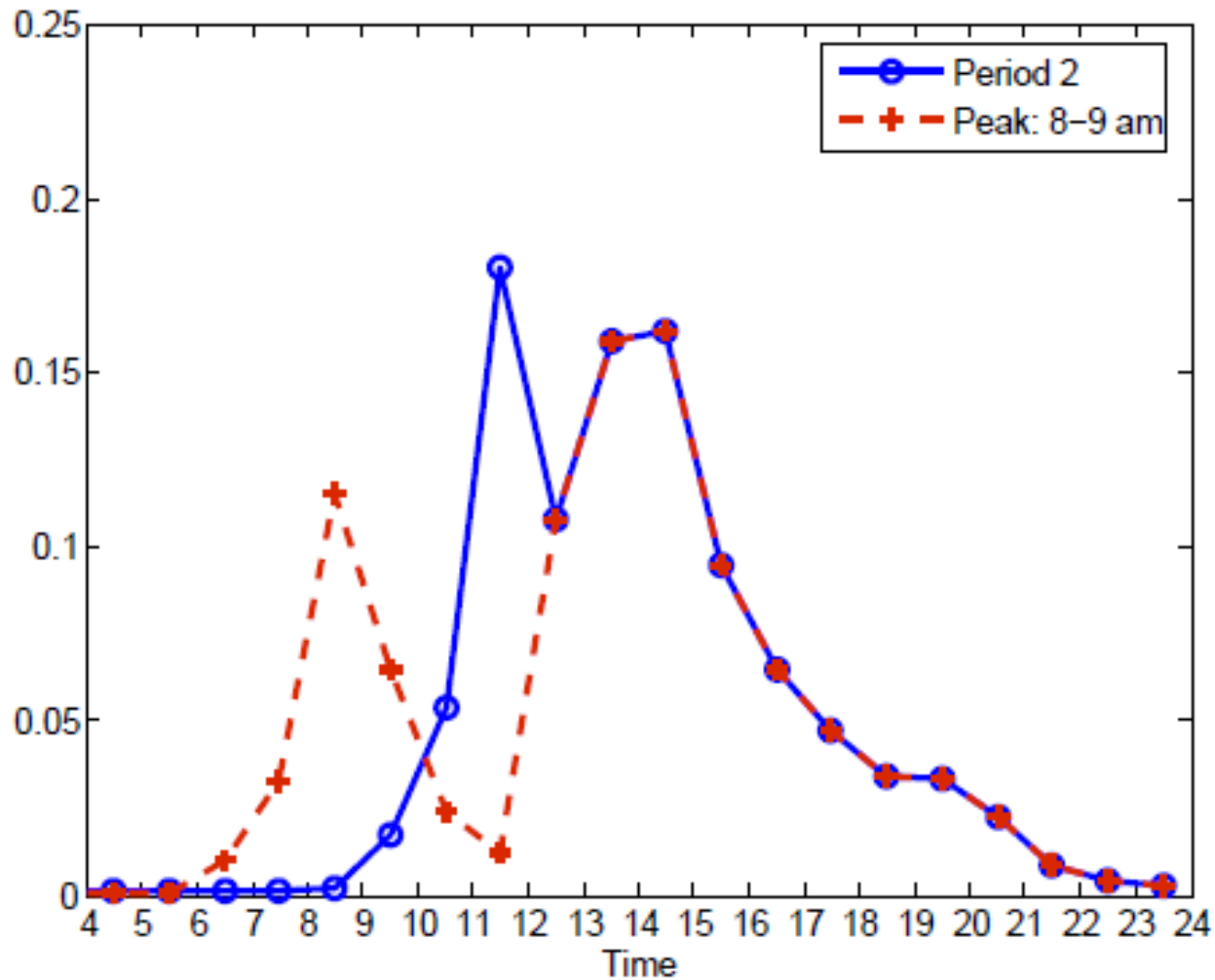
- Simulation shows the early discharge policy has little improvement

(a) hourly avg. waiting time

(b) 6-hour service level



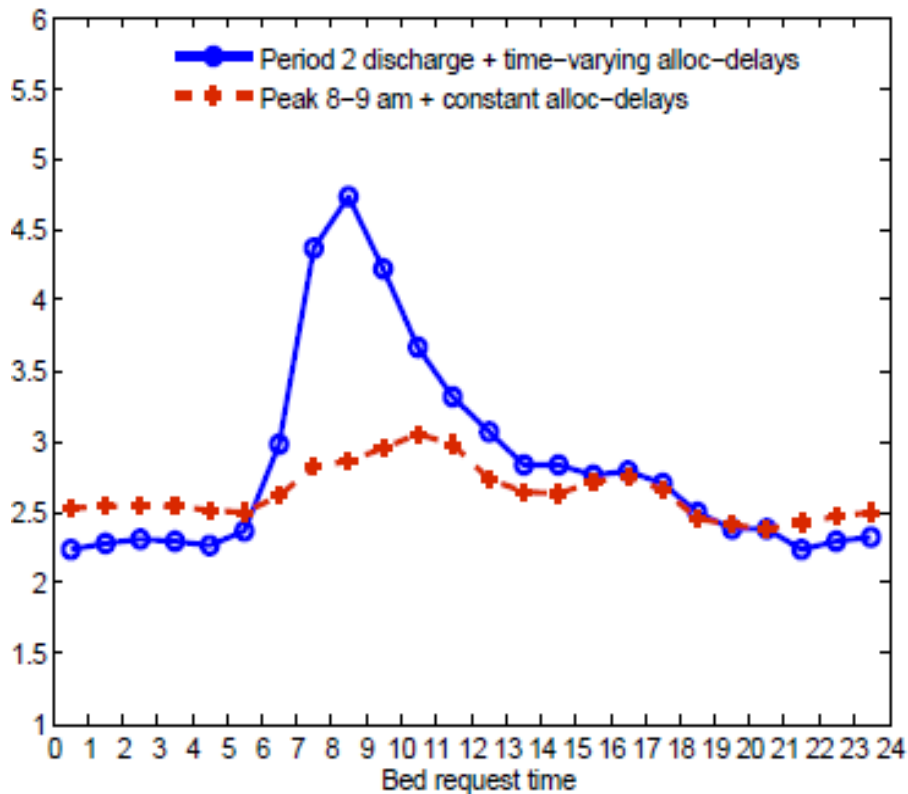
# Aggressive early discharge policy



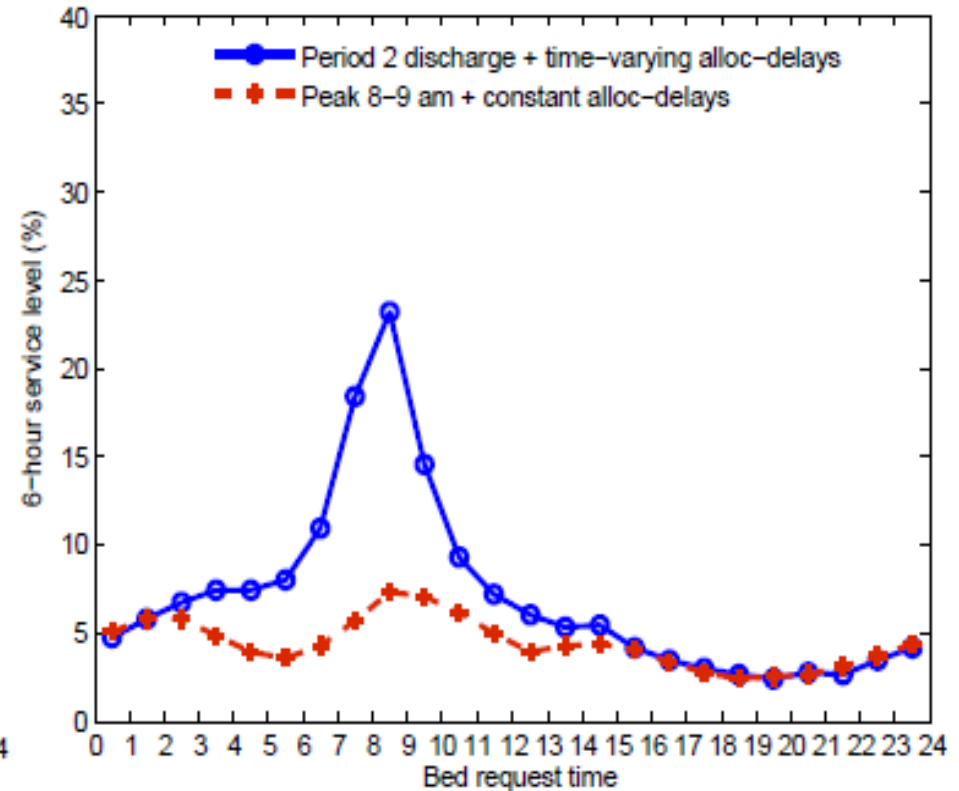
# Aggressive early discharge + smooth allocation delay

- Waiting time performances can be stabilized

(a) hourly avg. waiting time



(b) 6-hour service level

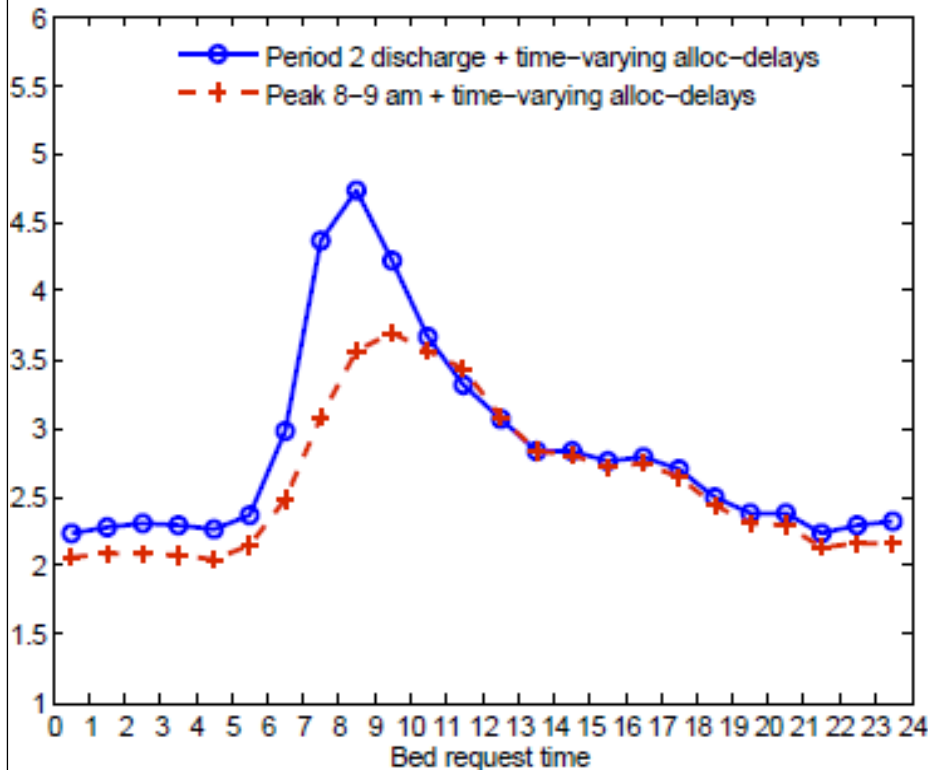




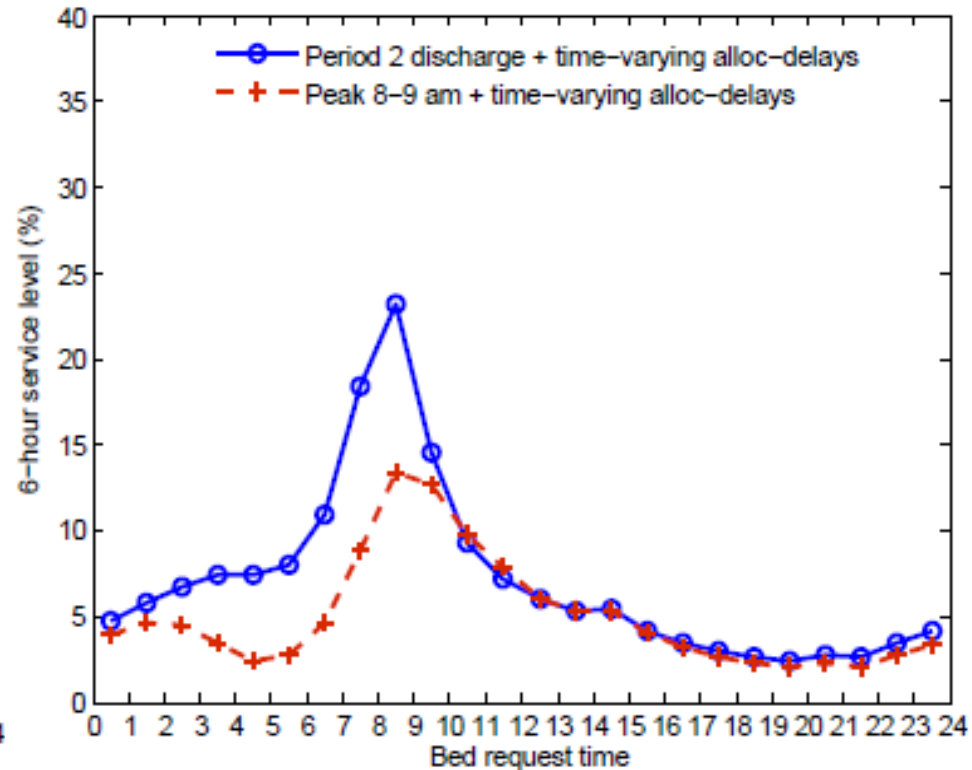
# Only use aggressive early discharge

- Cannot be stabilized

(a) hourly avg. waiting time



(b) 6-hour service level

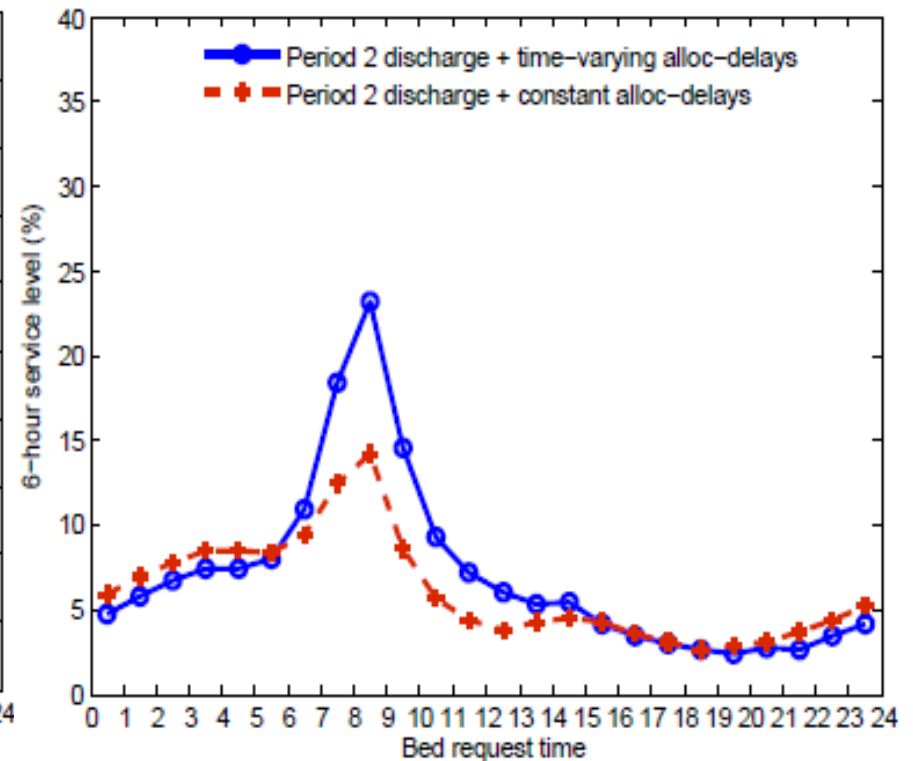
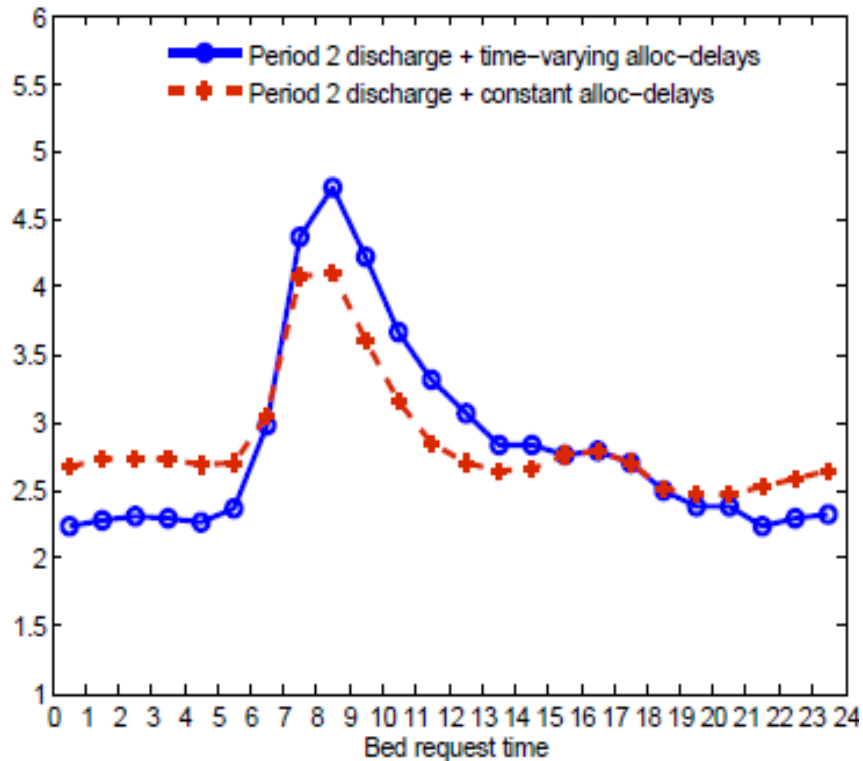


# Only smooth the allocation delays

- Assuming allocation delay has a constant mean

(a) hourly avg. waiting time

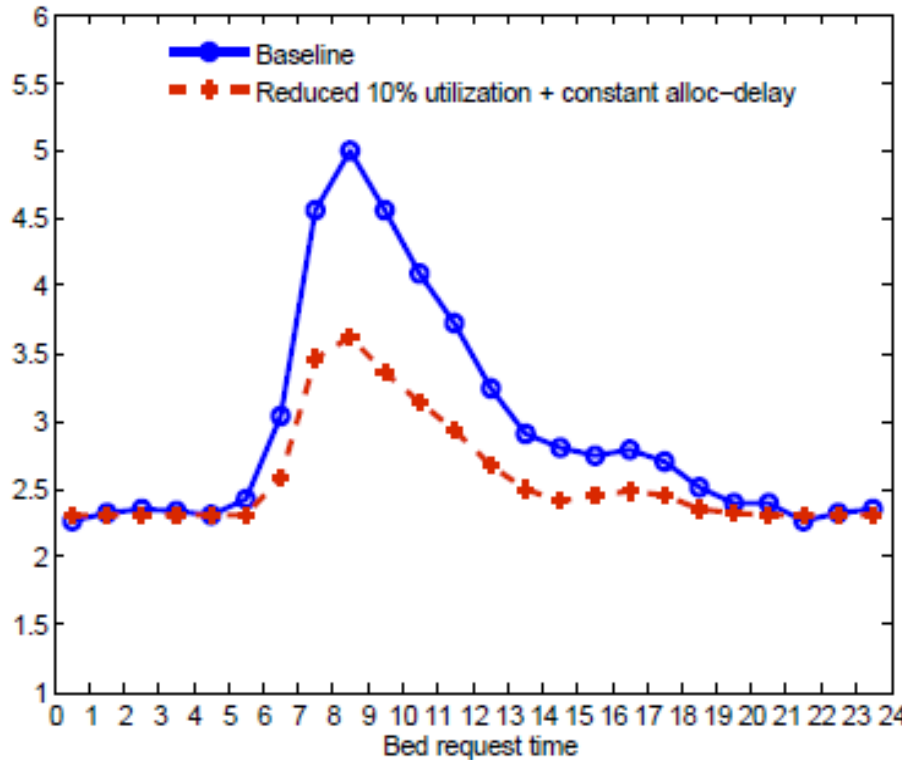
(b) 6-hour service level



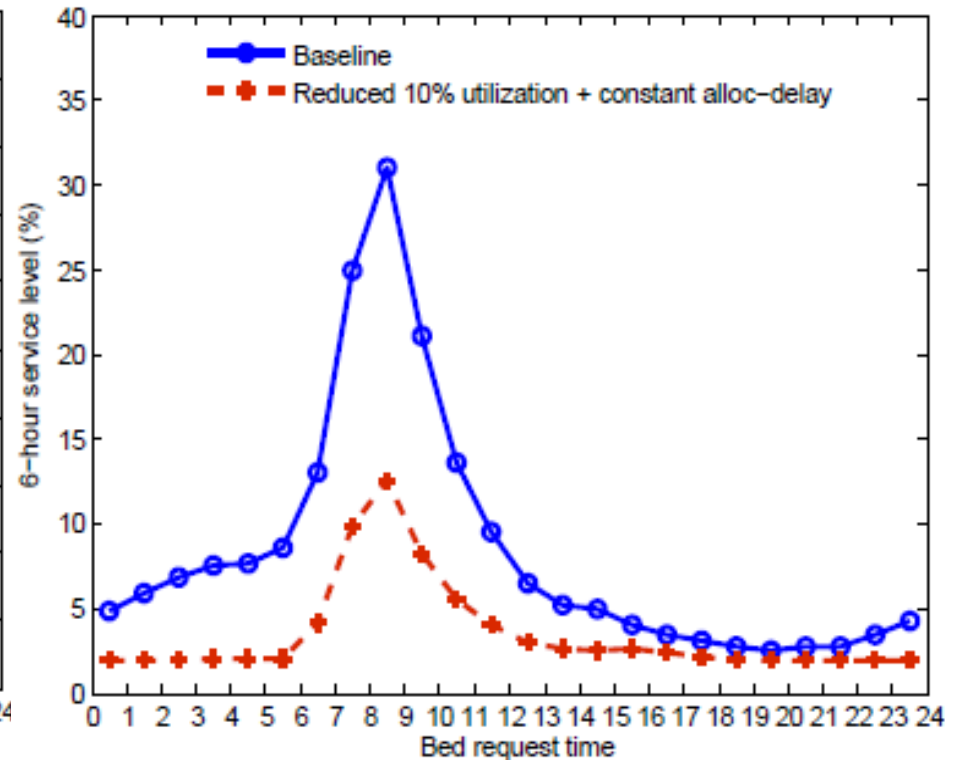
# Impact of capacity increase

- 10% reduction in utilization, plus assuming allocation delay has a constant mean

(a) hourly avg. waiting time



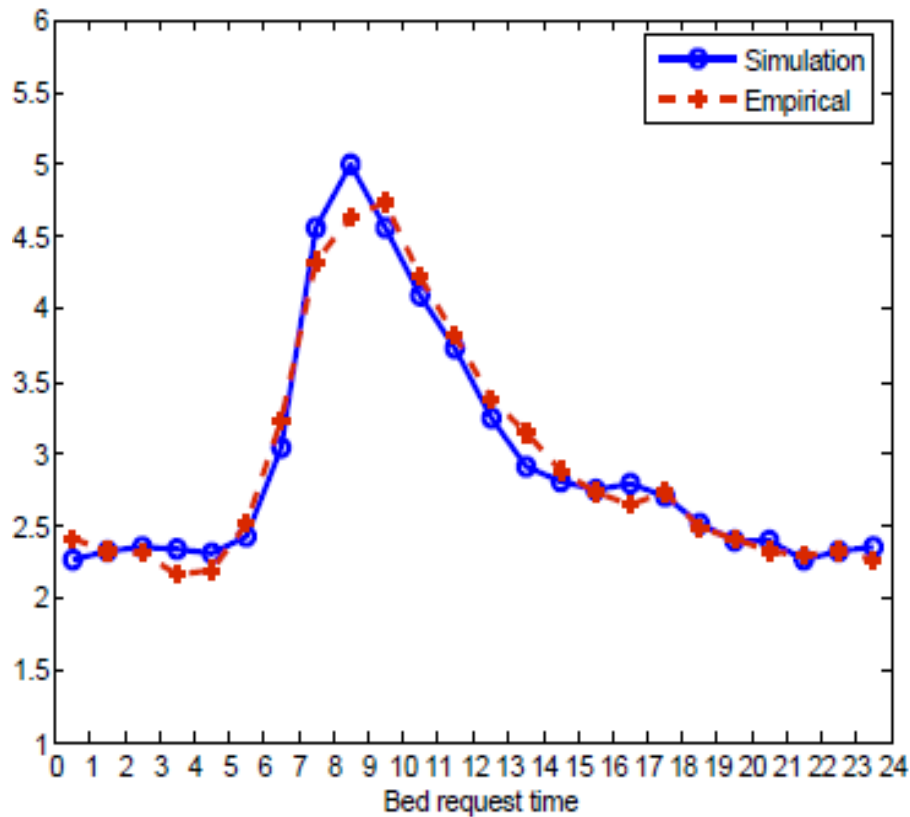
(b) 6-hour service level



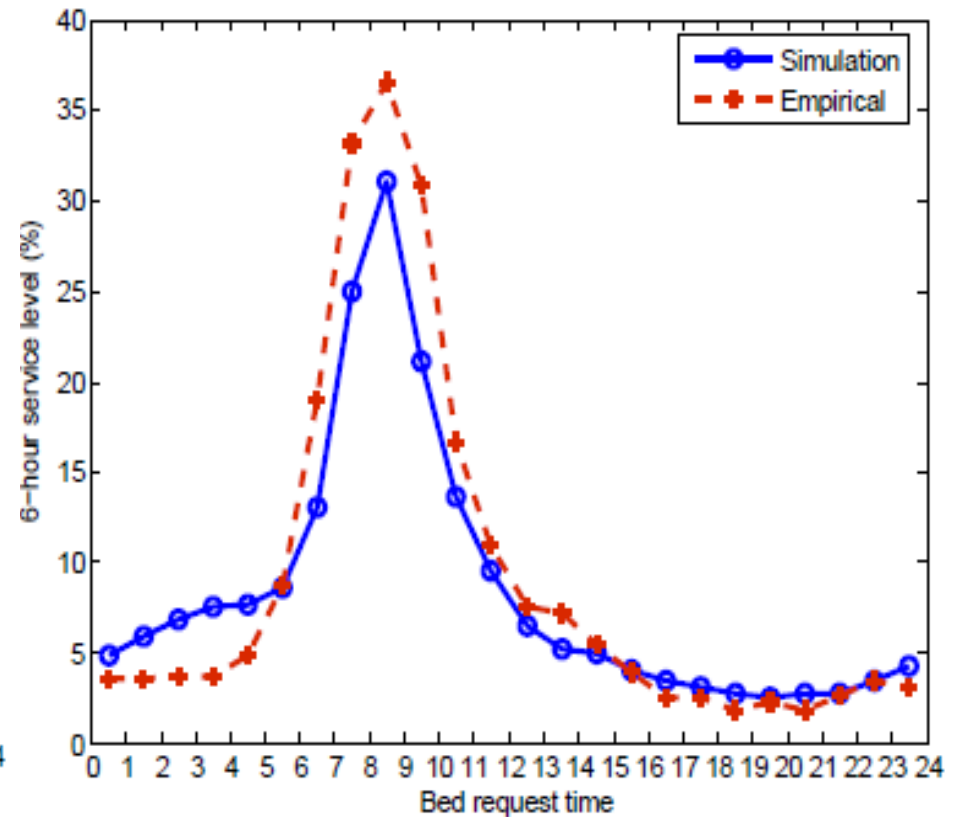
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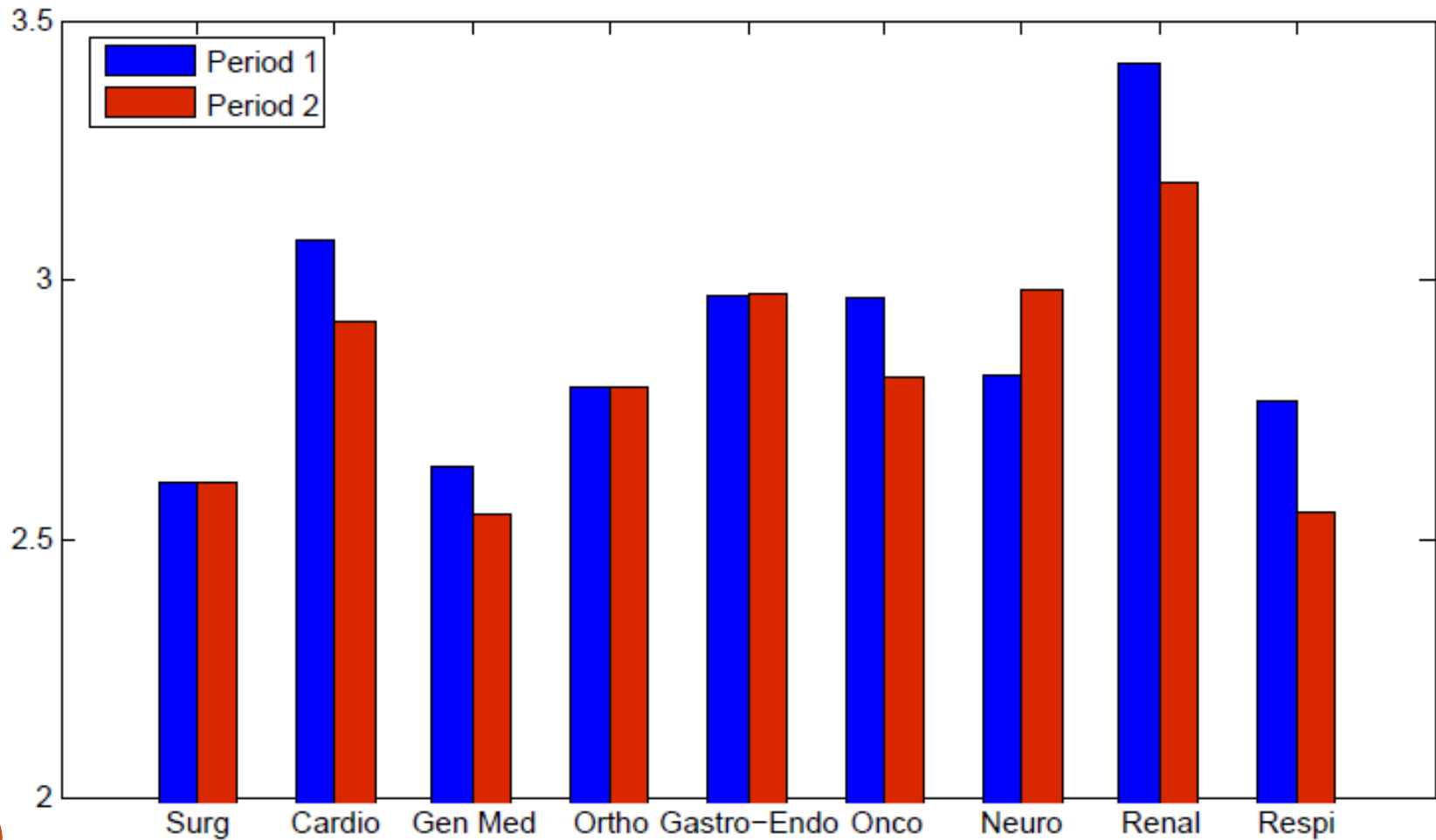


(b) Hourly 6-hour service level



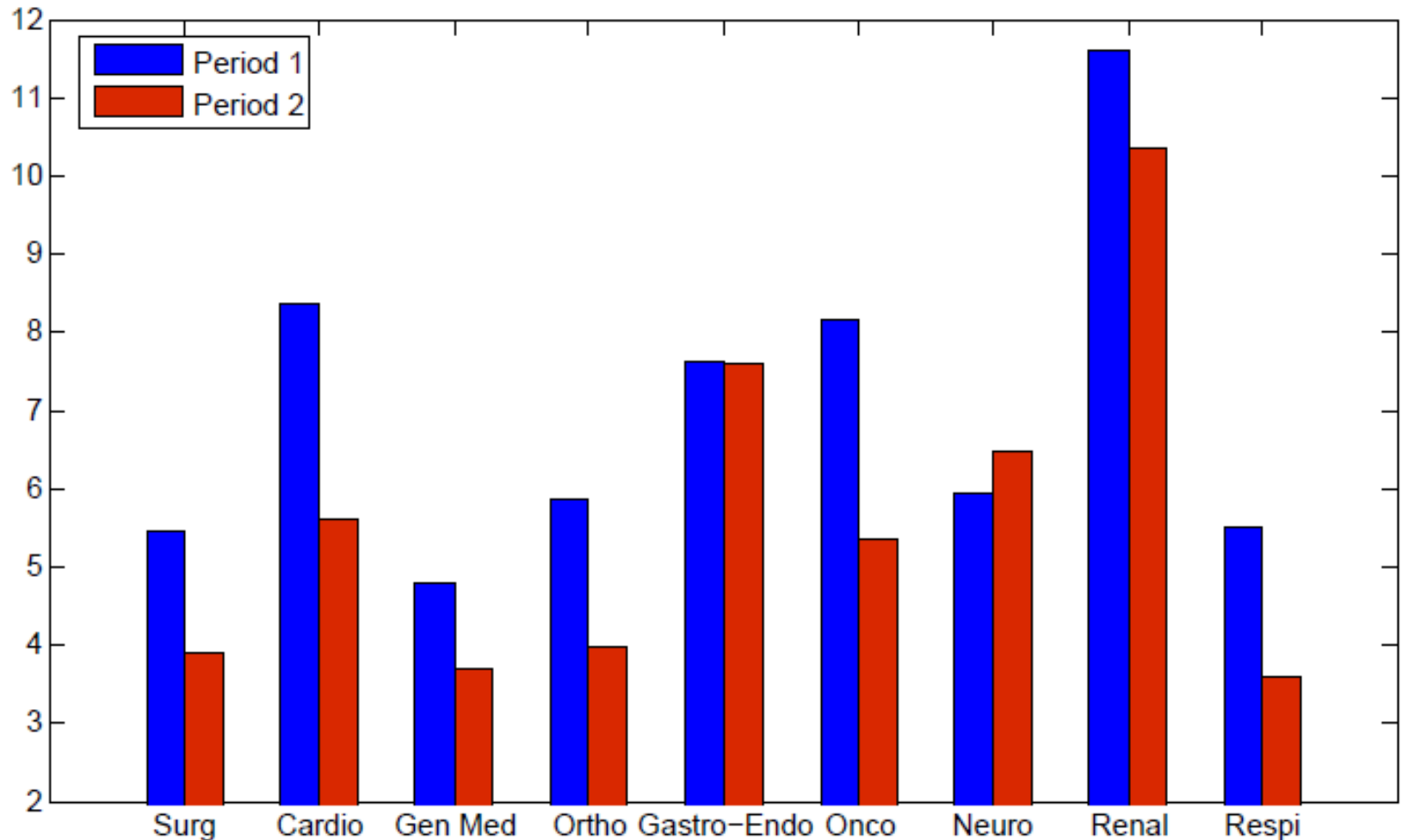
# Average waiting time for each specialty

- Renal patients have longest average waiting time



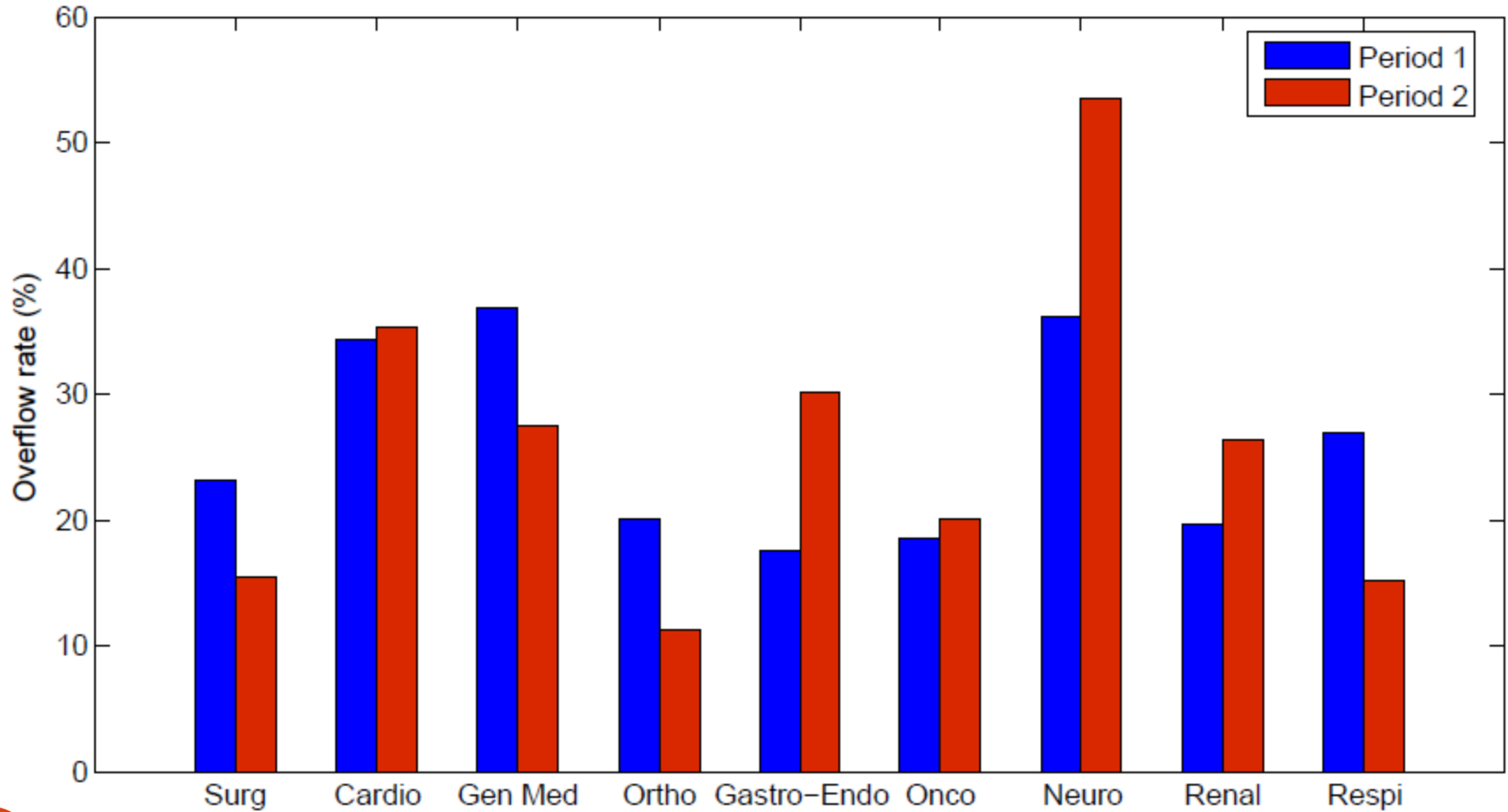
# 6-hour service level for each specialty

- Cardio and Oncology patients show significant improvement in the 6-hour service level



# Overflow rate

- Overall overflow rate reduces in Period 2



# Summary

- Conduct an empirical study of patient flow of the entire inpatient department
- Build and calibrate a stochastic model to evaluate the impact of discharge distribution on waiting for admission to ward
- Identify allocation delays as a second source of bottlenecks
  - Staffing appropriately in BMU, ED and Ward
- Achieve stable waiting time by aggressive early discharge + smooth allocation delay



# Limitations

- Simulation cannot fully calibrate with the overflow rate
  - Bed class (A, B, C)
  - Gender mismatch
  - Hospital acquired infections
    - Example: a female Surg patient has to be overflowed to a Med ward, since the only available Surg beds are for males
- Day-of-week phenomenon
  - Admission and discharge both depends on the day of week
  - LOS depends on admission day
  - Performances (BOR, waiting time) varies among days

Questions?