

Example:

| Period (i) | Demand (d _i) | Production cost (c _i) | Fixed cost (f _i) | Holding cost (h _i) |
|------------|--------------------------|-----------------------------------|------------------------------|--------------------------------|
| 1 | 10 | 3 | 5 | 0.2 |
| 2 | 40 | 2 | 20 | 0.3 |
| 3 | 20 | 4 | 10 | 0.5 |
| 4 | 50 | 3 | 10 | 0.8 |

Notes

Summary of DP Computation:

| Possible States (i) | Stage 5 | Stage 4 | | Stage 3 | | Stage 2 | | Stage 1 | |
|---------------------|---------------------|---------------------|-----------------|---------------------|-----------------|---------------------|-----------------|---------------------|-----------------|
| | f* ₅ (i) | f* ₄ (i) | x* ₄ | f* ₃ (i) | x* ₃ | f* ₂ (i) | x* ₂ | f* ₁ (i) | x* ₁ |
| 0 | 0 | 160 | 50 | 250 | 20 | 286 | 110 | 321 | 10 |
| 10 | 0 | 130 | 40 | 210 | 10 | 266 | 100 | | |
| 20 | 0 | 100 | 30 | 160 | 0 | 246 | 90 | | |
| 30 | 0 | 70 | 20 | 135 | 0 | 226 | 80 | | |
| 40 | 0 | 40 | 10 | 110 | 0 | 206 | 70 | | |
| 50 | 0 | 0 | 0 | 85 | 0 | 186 | 60 | | |
| 60 | 0 | | | 60 | 0 | 166 | 0 or 50 | | |
| 70 | 0 | | | 25 | 0 | 144 | 0 | | |
| 80 | 0 | | | | | 122 | 0 | | |
| 90 | 0 | | | | | 100 | 0 | | |
| 100 | 0 | | | | | 78 | 0 | | |
| 110 | 0 | | | | | 46 | 0 | | |

Hence, the optimal decision (quantity to produce in each period):

$$x_1 = 10$$

$$x_2 = 110$$

$$x_3 = 0$$

$$x_4 = 0$$

with the corresponding total cost = 321